

Looking at some data

	<u>Color</u>	<u>Size</u>	<u>Shape</u>	<u>Edible?</u>	
	Yellow	Small	Round	+	
	Yellow	Small	Round	-	
	Green	Small	Irregular	+	
	Green	Large	Irregular	-	
	Yellow	Large	Round	+	
	Yellow	Small	Round	+	
	Yellow	Small	Round	+	
	Yellow	Small	Round	+	
	Green	Small	Round	-	
	Yellow	Large	Round	-	
	Yellow	Large	Round	+	
	Yellow	Large	Round	-	
	Yellow	Large	Round	-	
	Yellow	Large	Round	-	
	Yellow	Small	Irregular	+	
	Yellow	Large	Irregular	+	
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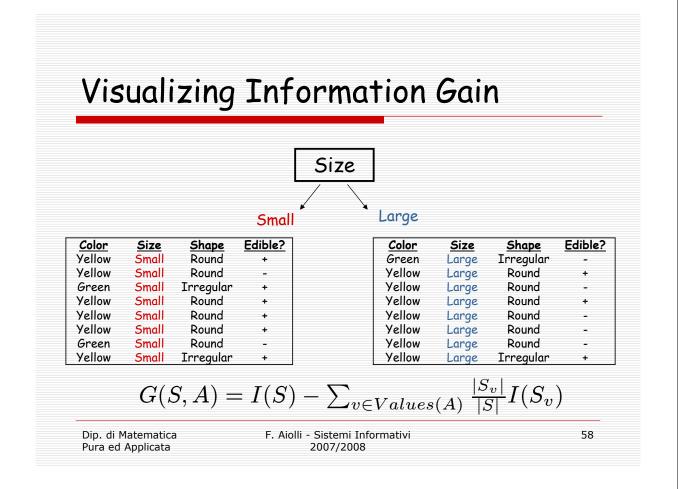
Entropy for our data set

□ 16 instances: 9 positive, 7 negative.

$$I(all_data) = -\left[\left(\frac{9}{16}\right)\log_2\left(\frac{9}{16}\right) + \left(\frac{7}{16}\right)\log_2\left(\frac{7}{16}\right)\right]$$

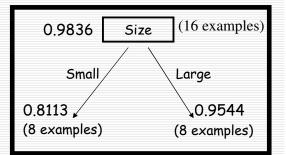
□ This equals: 0.9836

This makes sense - it's almost a 50/50 split; so, the entropy should be close to 1.



Visualizing Information Gain

The data set that goes down each branch of the tree has its own entropy value. We can calculate for each possible attribute its **expected entropy**. This is the degree to which the entropy would change if branch on this attribute. You **add** the entropies of the two children, **weighted** by the proportion of examples from the parent node that ended up at that child.



Entropy of left child is <u>0.8113</u> I(size=small) = 0.8113

Entropy of right child is <u>0.9544</u> I(size=large) = 0.9544

$I(S_{Size}) = (8/16)^{*}.8113 + (8/16)^{*}.9544 = .8828$

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G(attrib) = I(parent) - I(attrib)

We want to calculate the <u>information gain</u> (or entropy reduction). This is the reduction in 'uncertainty' when choosing our first branch as 'size'. We will represent information gain as "G."

 $G(size) = I(S) - I(S_{Size})$ G(size) = 0.9836 - 0.8828G(size) = 0.1008

> <u>Entropy</u> of all data at parent node = **I(parent)** = 0.9836 Child's <u>expected entropy</u> for '**size'** split = **I(size)** = 0.8828

So, we have gained 0.1008 *bits* of information about the dataset by choosing 'size' as the first branch of our decision tree.

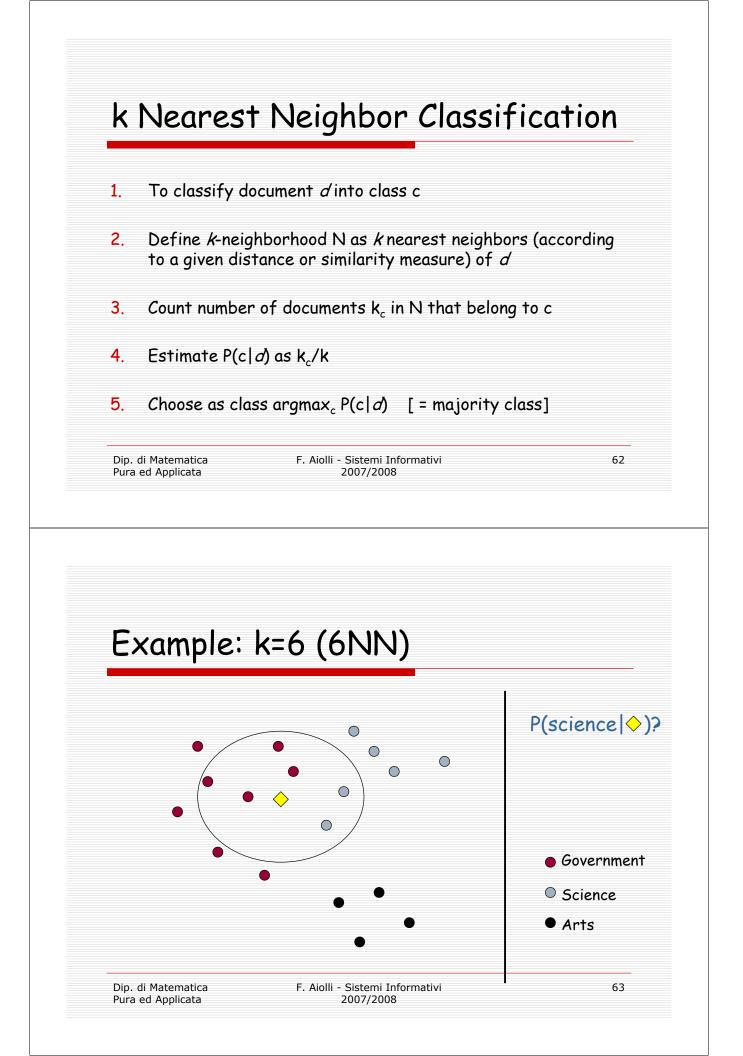
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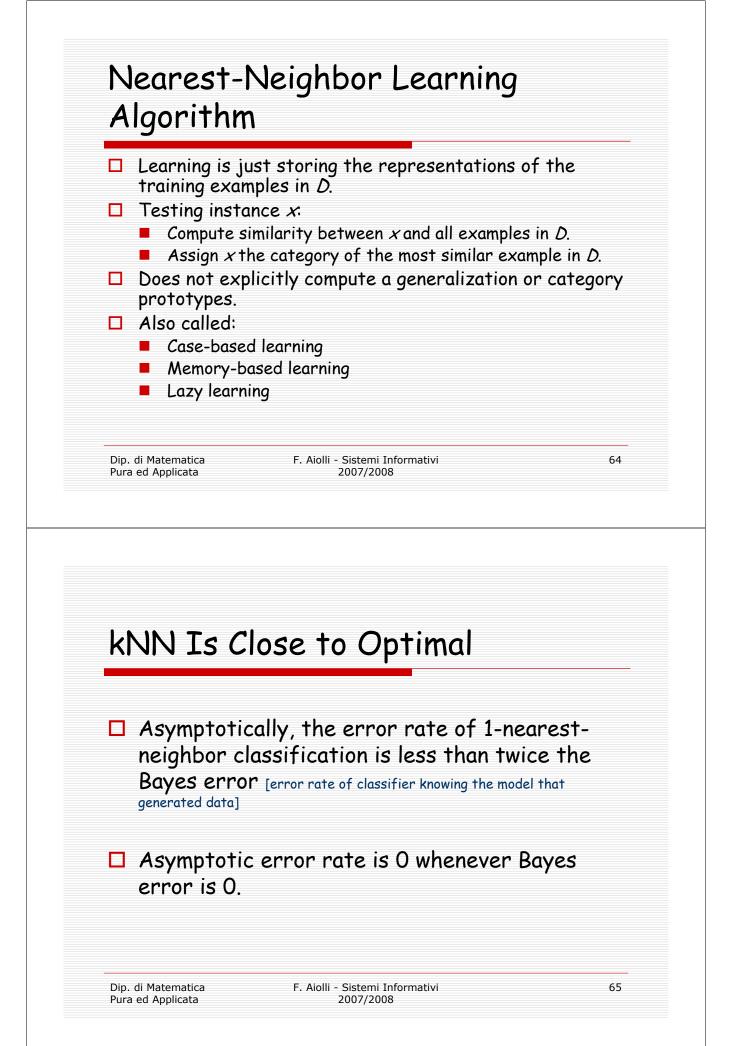
Example-based Classifiers

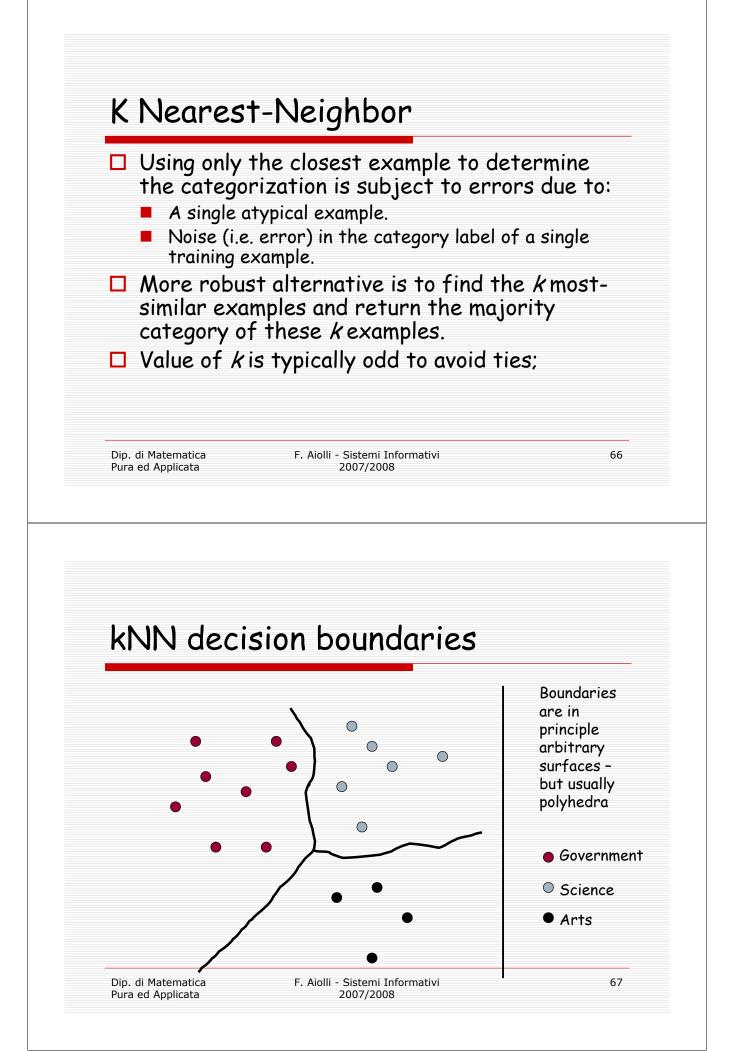
Example-based classifiers (EBCs) learns from the categories of the training documents similar to the one to be classified

The most frequently used EBC is the k-NN algorithm

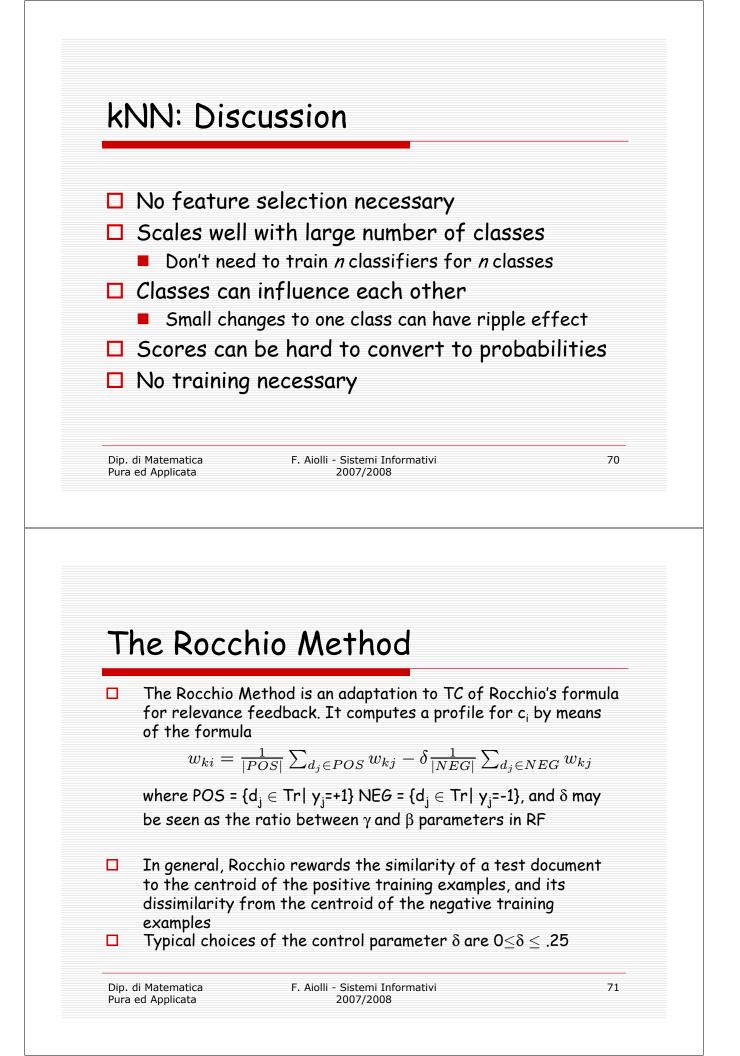
60

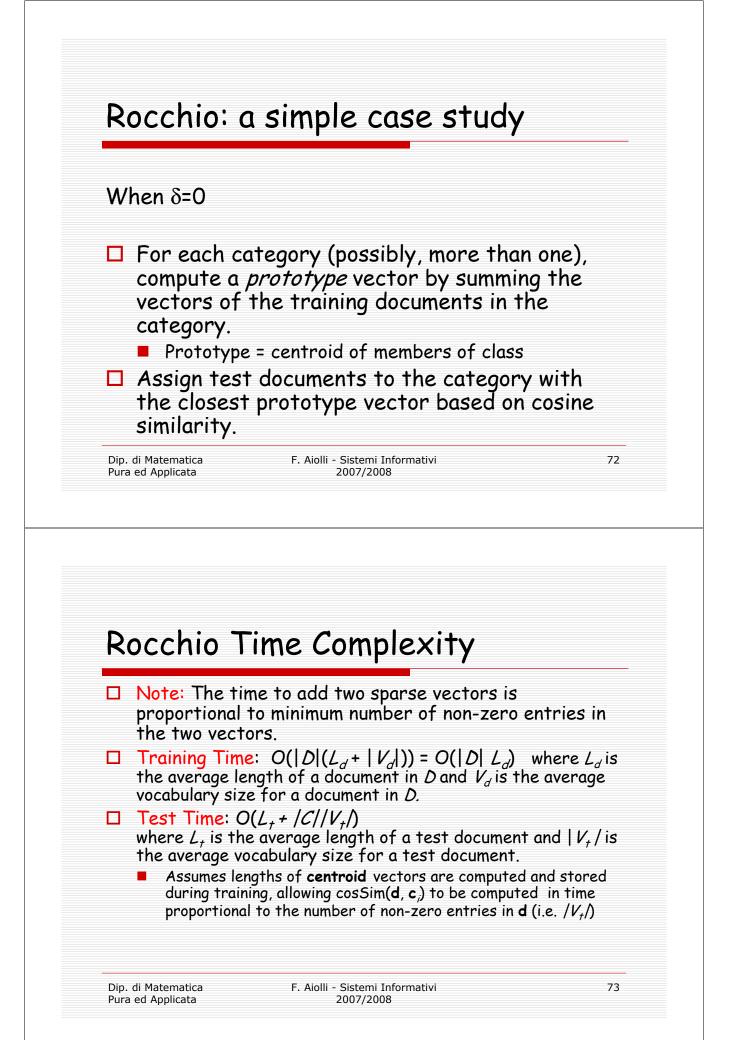


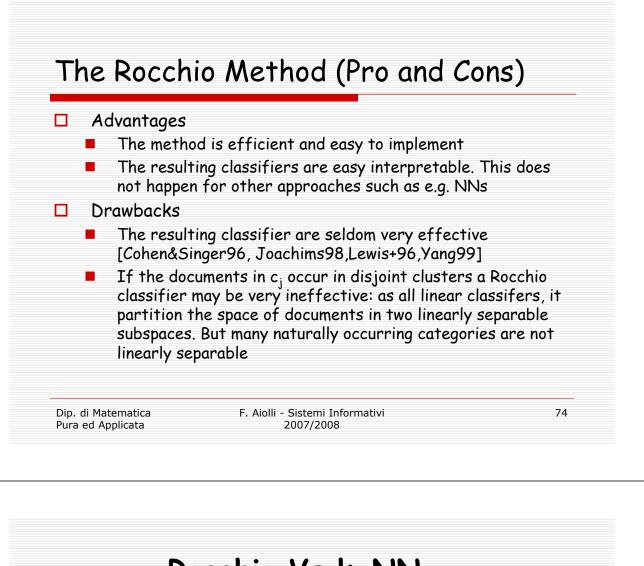


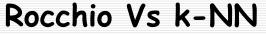


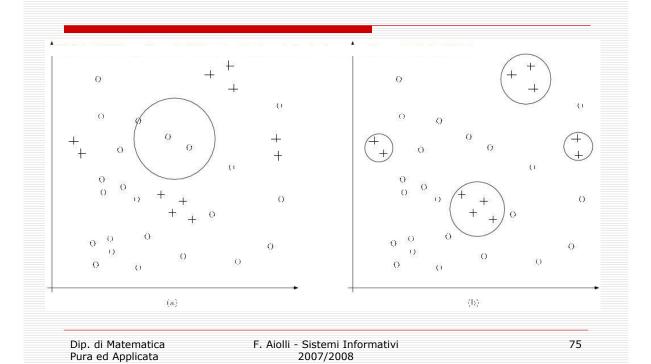
 similarity (or distance) metric. Simplest for continuous <i>m</i>-dimensional instance space is <i>Euclidian distance</i>. Simplest for <i>m</i>-dimensional binary instance space is <i>Hamming distance</i> (number of feature values that differ). For text, cosine similarity of tf.idf weighted vectors is typically most effective. But any metric can be used!! 	
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Nearest Neighbor with Inverted	
Index	
Naively finding nearest neighbors requires a linear	
Naively finding nearest neighbors requires a linear search through D documents in collection	
But determining k nearest neighbors is the same as determining the k best retrievals using the test	
document as a query to a database of training	
documents.	
Use standard vector space inverted index methods to find the k nearest neighbors.	1
Testing Time: $O(B/V_t/)$ where B is the average	
number of training documents in which a test-document wor appears.	rd











Instead of considering the set of negative training instances in its entirely, a set of near-positives might be selected (as in RF). This is called the query zoning method
Near positives are more significant, since they are the most difficult to tell apart from the positives. They may be identified by issuing a Rocchio query consisting of the centroid of the positive training examples against a document base consisting of the negative training examples. The top-ranked ones can be used as near positives.
Some claim that, by using query zones plus other enhancements, the Rocchio method can achieve levels of effectiveness comparable to state-of-the art methods while being quicker to train
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