

The dendogram

The y-axis of the dendogram represents the combination similarities, i.e. the similarities of the clusters merged by a the horizontal lines for a particular y

□ Assumption: The merge operation is monotonic, i.e. if $s_1,..,s_{k-1}$ are successive combination similarities, then $s_1 \ge s_2 \ge ... \ge s_{k-1}$ must hold

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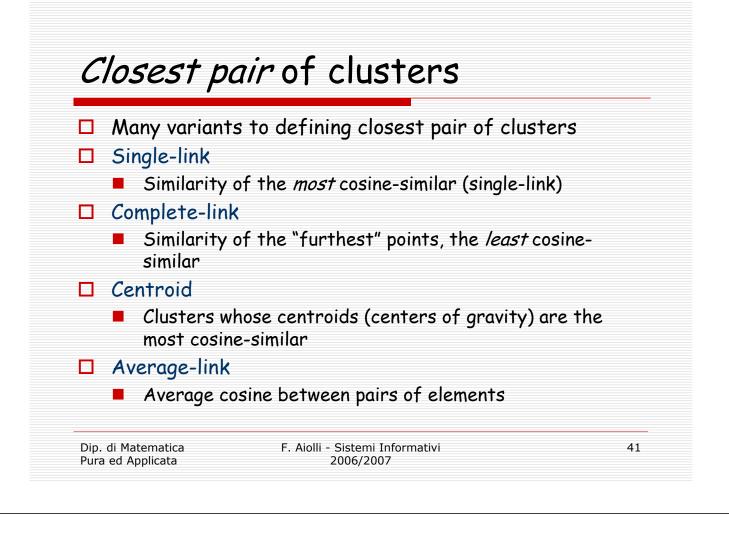
Hierarchical Agglomerative Clustering (HAC)

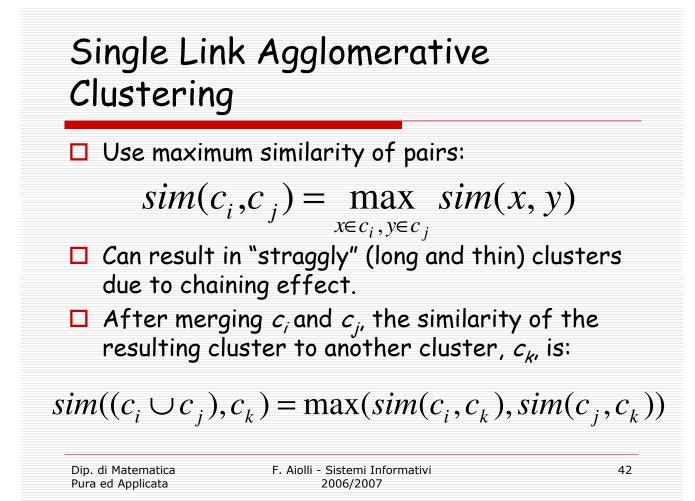
□ Starts with each doc in a separate cluster

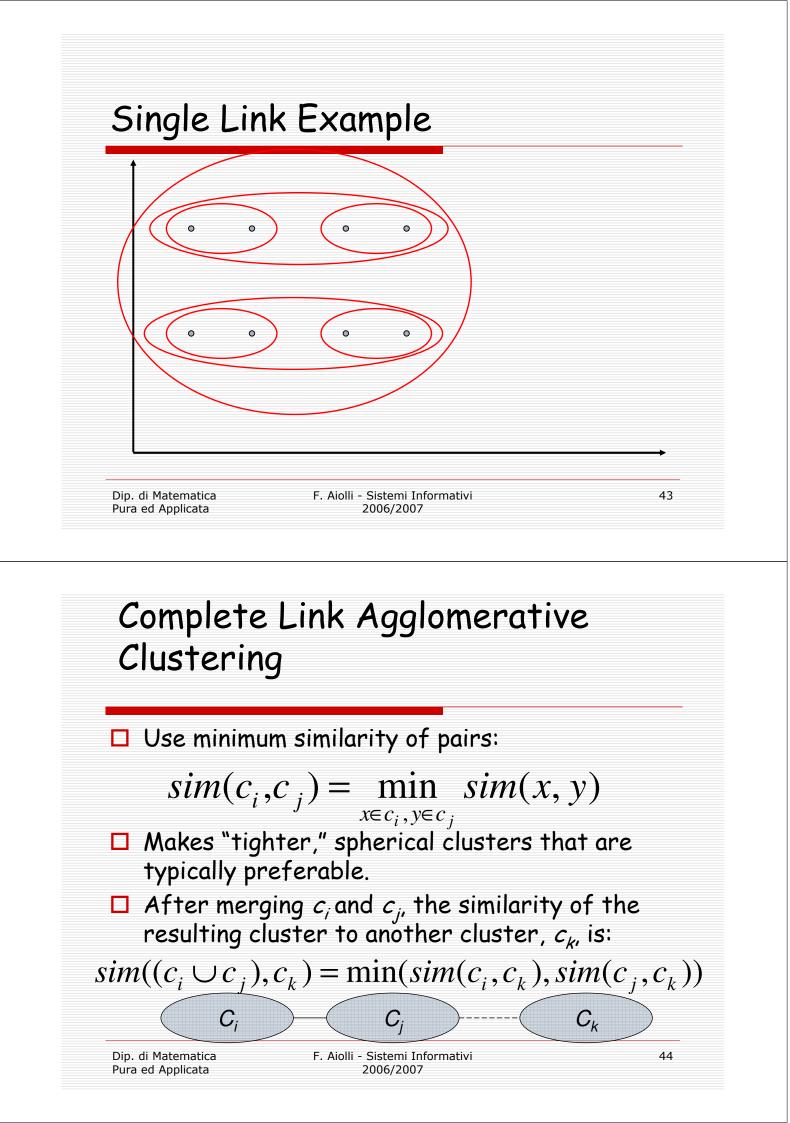
then repeatedly joins the closest pair of clusters, until there is only one cluster.

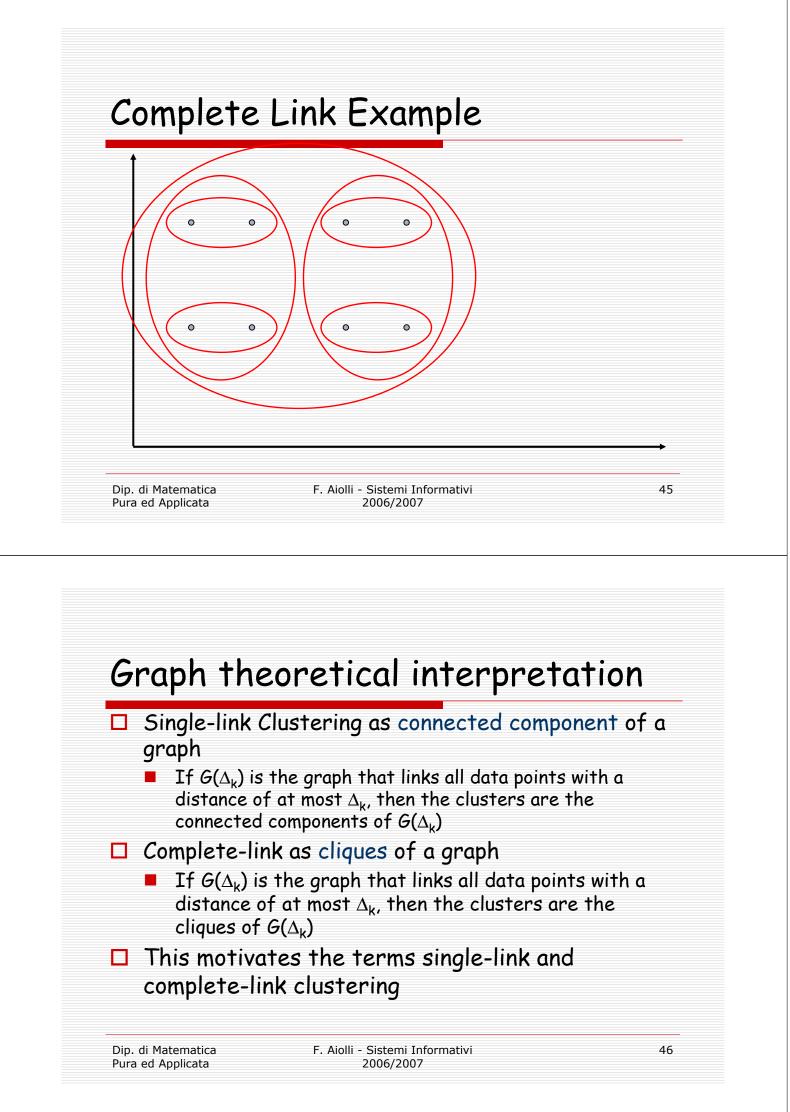
The history of merging forms a binary tree or hierarchy.

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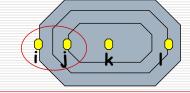




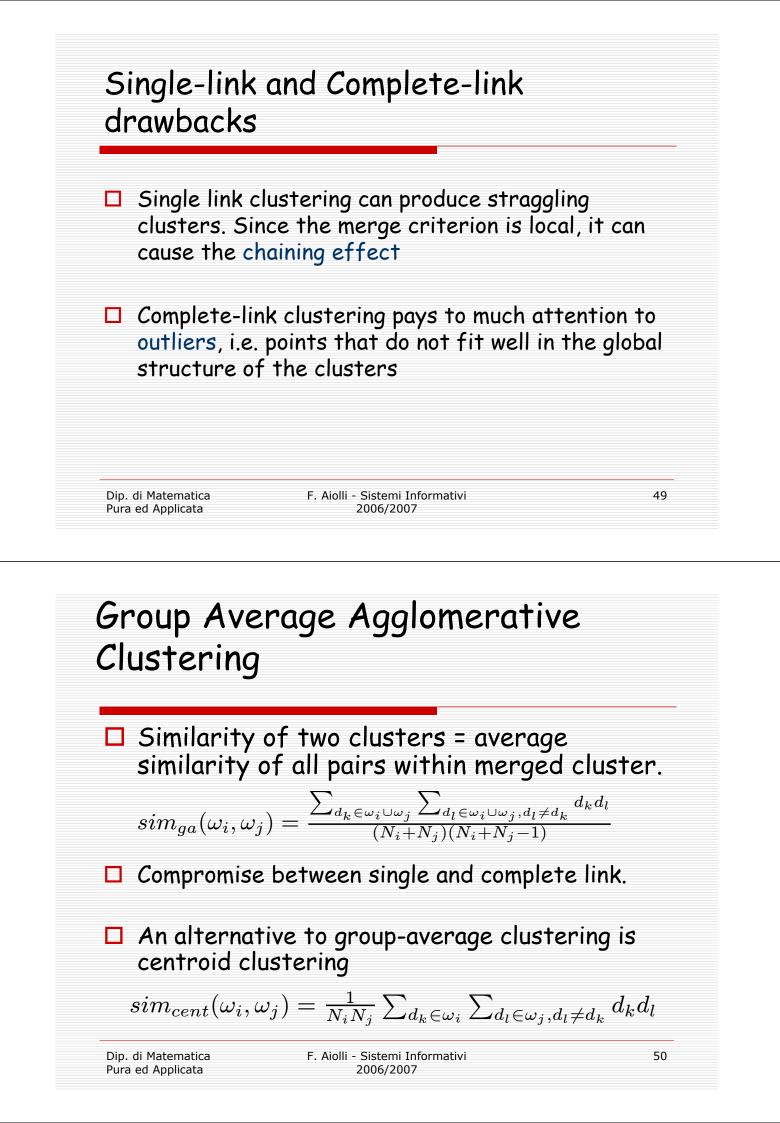
In the first iteration, all HAC methods need to compute similarity of all pairs of n individual instances which is $O(n^2)$.				
In each of the subsequent n -2 merging iterations, compute the distance between the most recently created cluster and all other existing clusters.				
computing si	naintain an overall O(<i>n</i> ²) perfor milarity to each other cluster m			
in constant t Else O(n²) 	log n) or O(n³) if done naively			

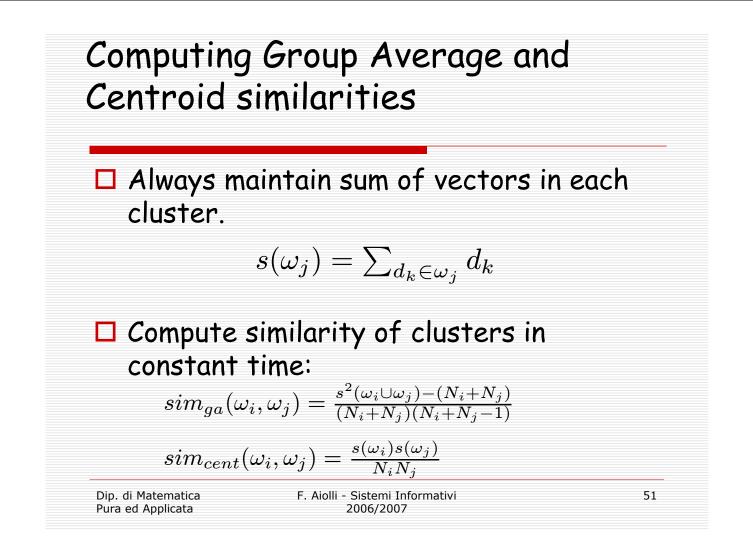
Best-Merge Persistency

- The single-link agglomerative clustering is bestmerge persistent
- Suppose that the best merge cluster for k is j
- □ Then, after merging j with a third cluster i ≠ k, the merger of i and j will be the k's best merge cluster
- As a consequence, we can keep the best merge candidates for the merged cluster as one of the two best merge candidates for the merged clusters



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Summarizing

Single-link	Max sim of any two points	O(N ²)	Chaining effect
Complete-link	Min sim of any two points	O(N ² logN)	Sensitive to outliers
Centroid	Similarity of centroids	O(N ² logN)	Non monotonic
Group- average	Avg sim of any two points	O(N ² logN)	ОК

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