

Exercise. Consider a CCS process that models a 1-place buffer, i.e., a memory cell that can contain a single value: it receives the value on channel **in**, it stores it and it delivers the value on channel **out**:

$$\begin{aligned} C &\stackrel{\text{def}}{=} \mathbf{in}(x).C'(x) \\ C'(x) &\stackrel{\text{def}}{=} \overline{\mathbf{out}}(x).C \end{aligned}$$

Use the C process to implement

1. An (unordered) buffer with capacity 2, with the following behavior:

$$\begin{aligned} B_2 &\stackrel{\text{def}}{=} \mathbf{in}(x).B_1(x) \\ B_1(x) &\stackrel{\text{def}}{=} \mathbf{in}(y).B_0(x, y) + \overline{\mathbf{out}}(x).B_2 \\ B_0(x, y) &\stackrel{\text{def}}{=} \overline{\mathbf{out}}(x).B_1(y) + \overline{\mathbf{out}}(y).B_1(x) \end{aligned}$$

2. A FIFO buffer with capacity 2, with the following behaviour:

$$\begin{aligned} F_2 &\stackrel{\text{def}}{=} \mathbf{in}(x).F_1(x) \\ F_1(x) &\stackrel{\text{def}}{=} \mathbf{in}(y).F_0(x, y) + \overline{\mathbf{out}}(x).F_2 \\ F_0(x, y) &\stackrel{\text{def}}{=} \overline{\mathbf{out}}(x).F_1(y) \end{aligned}$$