

# Formal methods ... in Action!

## typestate-oriented actor programming in Scala akka

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In distributed systems the  
***coordination of concurrent entities***  
is a key issue



## Protocol-Oriented Programming

*thinking* (hence programming)  
*in terms of*  
communication *protocols*

it requires:

- **high-level support to declare/express** the coordination protocol
- **support to check it!** ...hopefully statically...(gradual) typing?



# **TypeState-Oriented** Programming

# TypeState-oriented OOP

Strom, Yemini '86  
DeLine, Fahndrich '04  
Aldrich et al. '09

```
class File {  
    public void open(){ ... }  
    public int read(){ ... }  
    public void write(int i){ ... }  
    public close(){ ... }  
}
```

**interface**  
**vs**  
**protocol**

```
File f = ... //initialize
```

```
f.open(); f.write(5); f.close();
```



```
f.write(5); f.open(); f.read();
```



*wrong* protocol

```
f.open(); f.write(5);
```



*incomplete* protocol

# TypeState-oriented OOP

a `File` has two possible **states**: `CLOSED`, `OPEN`

```
public void open() { ... } // move the state to OPEN
```

```
public int read() { ... }  
public void write(int i) { ... }  
public close() { ... } // move the state to CLOSED
```

a type system **statically** guarantees that **methods** are **invoked** when the object is in the **correct state**

## Mechanisms

- state annotations in types
- tracking of state transitions
- **aliasing control**



# TypeState-Oriented Programming

for **Concurrent** objects

concurrent objects are typically aliased  
state transitions aren't always statically trackable



# The Chemical Approach to Typestate-Oriented Programming

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a sound **behavioral type system**  
for the Objective *Join Calculus*



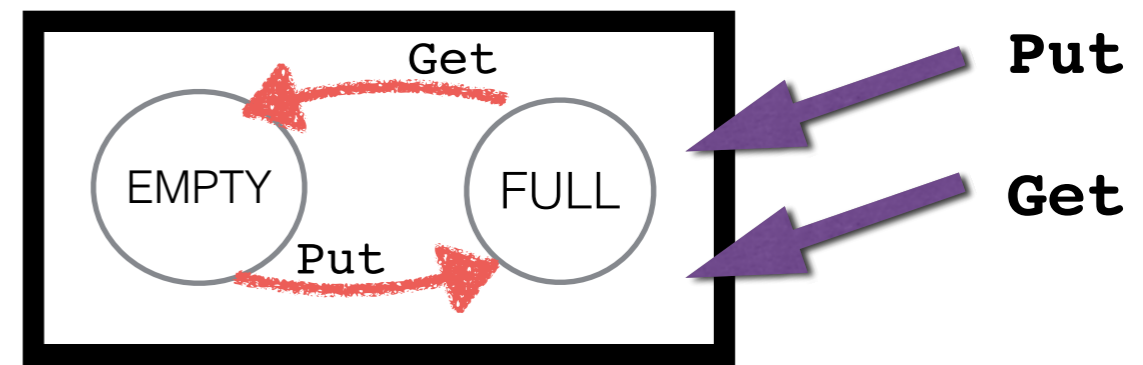
**both object **state** and object  
**messages** as *molecules***

## Chemical Abstract Machine:

- object **methods** are **join reactions** that consume molecules and produce new ones:
- **programs** are object definitions and a **soup** of molecules
- **runtime semantics** resolves races and executes methods at the right time

```
def a = m ► b.n
      or n ► a.m
in def b = m | n ► b.m
in a.m | a.n | b.m
```

# 1-place buffer



```
def buffer =  
    EMPTY | Put(v,r) ▶ buffer ! FULL(v) | r ! reply(buffer)  
or  
    FULL(v) | Get(r) ▶ buffer ! EMPTY | r ! reply(v,buffer)  
in  
    buffer ! EMPTY | // CONSTRUCTOR
```

```
let buffer = buffer ! Put(10)  
in let (v,buffer) = buffer ! Get  
in let buffer = buffer ! Put(20+v)  
in let (v,buffer) = buffer ! Get
```

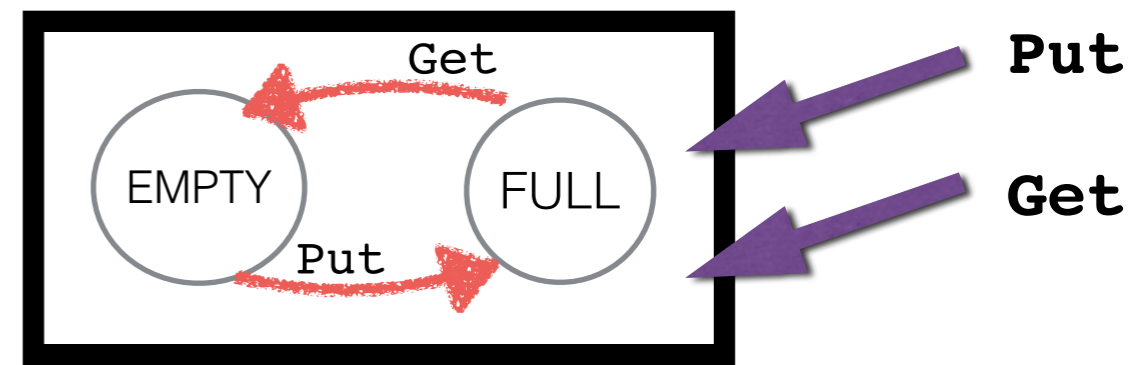
continuation-passing  
style

$$t_{\text{buff}} = (\text{EMPTY} \otimes t_{\text{EMPTY}}) \oplus (\text{FULL}(\text{int}) \otimes t_{\text{FULL}})$$
$$t_{\text{EMPTY}} = \text{Put}(\text{int}, \text{reply}(t_{\text{FULL}}))$$
$$t_{\text{FULL}} = \text{Get}(\text{reply}(\text{int}, t_{\text{EMPTY}}))$$

**behavioral type**  
with *linear connectives*



# 1-place buffer



```
def buffer =  
    EMPTY | Put(v,r) ▶ buffer ! FULL(v) | r ! reply(buffer)  
or  
    FULL(v) | Get(r) ▶ buffer ! EMPTY | r ! reply(v,buffer)  
in  
    buffer ! EMPTY | // CONSTRUCTOR
```

```
buffer!Put(10) & buffer!Put(20) & buffer!Put(30) | // PRODUCER  
buffer!Get & buffer!Get & buffer!Get // CONSUMER
```

runtime semantics will **execute**  
methods **at the right time**

$$t_{\text{buff}} = (\text{EMPTY} \oplus \text{FULL}(\text{int})) \otimes t_{\text{prod}} \otimes t_{\text{cons}}$$

$$t_{\text{prod}} = \text{Put}(\text{int}, \text{reply}(t_{\text{prod}}))$$

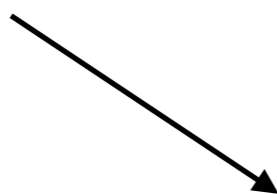
$$t_{\text{cons}} = \text{Get}(\text{reply}(\text{int}, t_{\text{cons}}))$$

# 1 object - **many** protocols / types



$t_{\text{buff}} = (\text{EMPTY} \oplus \text{FULL}) \otimes t_{\text{prod}} \otimes t_{\text{cons}}$

buffer : **t**



buffer : **t1**

$t_{\text{prod}} = \text{Put}(\text{int}, \text{reply}(t_{\text{prod}}))$

the **user** is **not aware of internal states**:  
it receives a reference whose **type** just  
express **how to use it**

# 1 object - **many** protocols / types



`buffer : t`



`buffer : t1`



`buffer : t2`

with  $t \leq t1, t2$

**subtyping:**

a super-type/protocol express a usage that is safe w.r.t.  $t$

## different from Session Types :

- there is **no strong duality** between the communicating parties
  - no fixed number of parties,
  - no precise protocol progression,
- in TSOP there is **asymmetry** between
  - the **object is stateful**
  - the **user(s)** receives a **typed handle** which prescribes **how to use the object**
- linear connectives allow *AND-states* and *OR-states*

## different from other TSOP approaches (e.g., Plaid, Mungo):

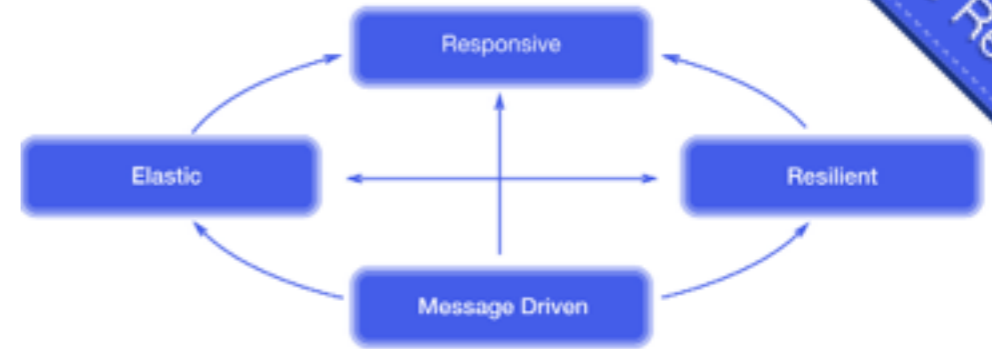
- **no state is exposed**, it is a private “molecule”
- hence there is **no need to control aliasing**
- but the **runtime synchronisation is essential** to keep messages and consume them at the right time

what about **mainstream**  
**distributed** systems  
programming?

# TypeState-Oriented Programming for **Concurrent** objects

Objective  
**Join Calculus**





We Are Reactive

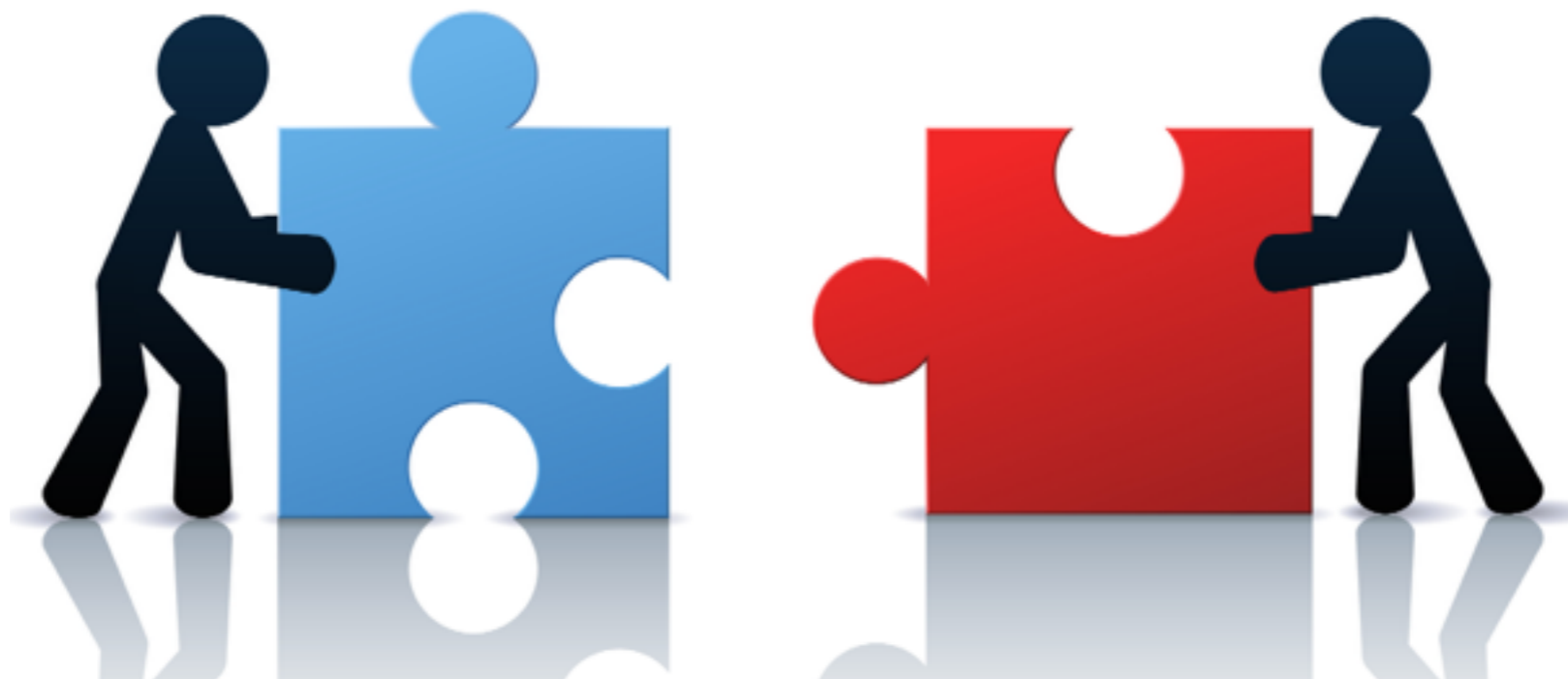
# Distributed Programming by means of **Actor systems**

more Object-Oriented than objects

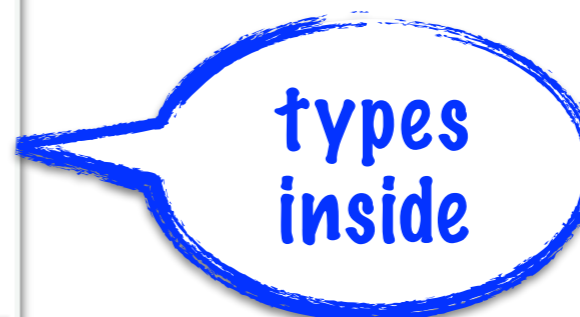
types  
inside

 **Scala**

 akka

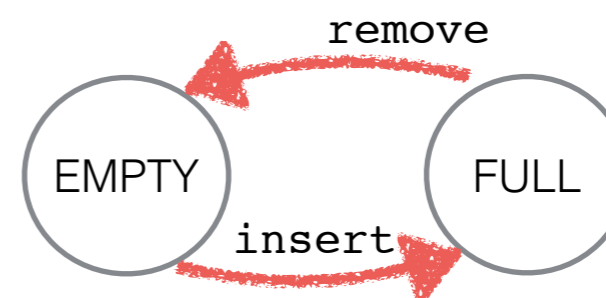


# **Protocol-Oriented** Distributed Programming as **TypeState-based Actor** programming



# 1-place buffer as TSOAP

```
case class insert[T](value:T)
case class remove()
```



```
class Buffer[T] extends Actor {
  def EMPTY:Receive = {
    case insert(x:T) => context.become(FULL(x))
  }

  def FULL(x:T):Receive = {
    case remove() => context.become(EMPTY)
  }

  def receive = EMPTY
}
```

**clean logic:**  
**each behaviour /state**  
**defines only the**  
**intended messages!**  
*no defensive*  
*programming*

```
val s = ActorSystem()
val buffer = s.actorOf(Props(new Buffer[Int]))
val user = s.actorOf(Props(new Actor{
  buffer ! insert(4)
  buffer ! remove()
}))
```



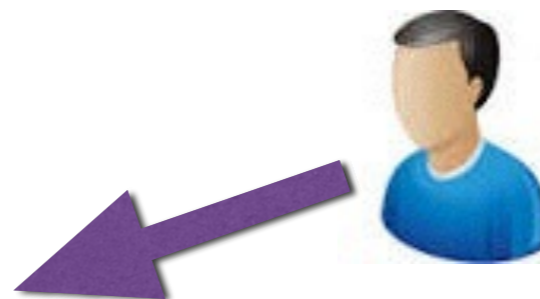
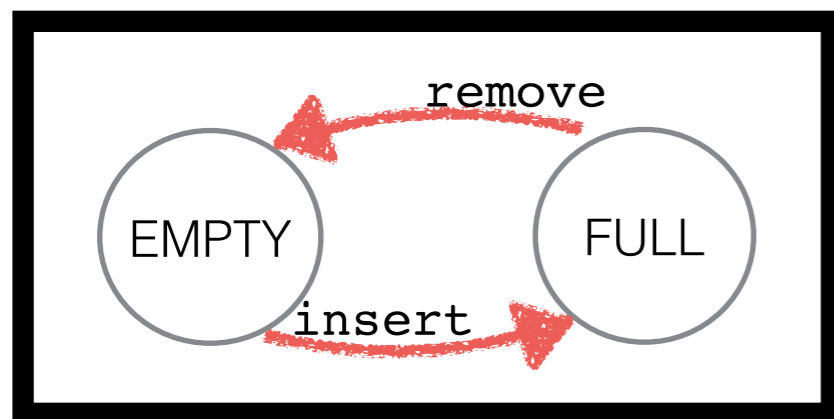


# 1-place buffer as TSOAP

```
class Buffer[T] extends Actor {  
  def EMPTY:Receive = {  
    case insert(x:T) => context.become(FULL(x))  
  }  
  def FULL(x:T):Receive = {  
    case remove() => context.become(EMPTY)  
  }  
  def receive = EMPTY  
}
```



**no support from the  
compiler**



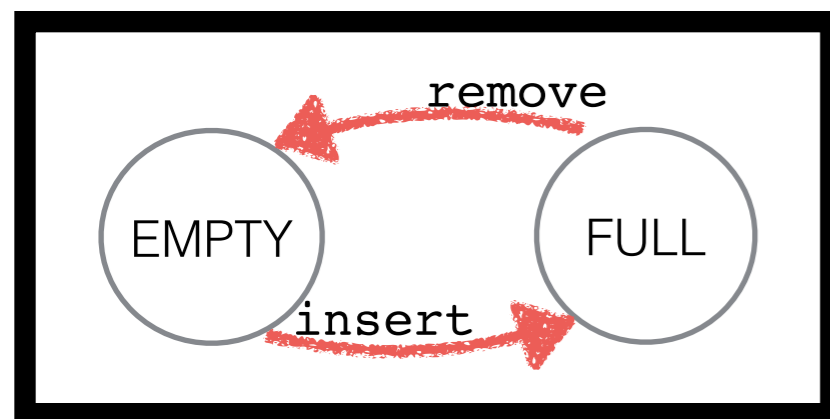
**bad msg!!**

~~buffer ! "hello"~~  
buffer ! insert(1)  
buffer ! remove()  
~~buffer ! remove()~~

**bad state!!**

# 1-place buffer as TSOAP

```
class Buffer[T] extends Actor {  
  def EMPTY:Receive = {  
    case insert(x:T) => context.become(FULL(x))  
  }  
  def FULL(x:T):Receive = {  
    case remove() => context.become(EMPTY)  
  }  
  def receive = EMPTY  
}
```



**Producer**



insert(1)  
insert(2)  
insert(3)  
...



remove()  
remove()  
remove()  
...

**Consumer**

**insert msg can arrive in the buffer's mailbox while the buffer is in state FULL !**

***we still want to ensure that insert / remove are served in the correct state!***



# 1-place buffer as TSOAP

```
class Buffer[T] extends Actor {  
  def EMPTY:Receive = {  
    case insert(x:T) => context.become(FULL(x))  
  }  
  def FULL(x:T):Receive = {  
    case remove() => context.become(EMPTY)  
  }  
  def receive = EMPTY  
}
```

add a layer of  
typing!

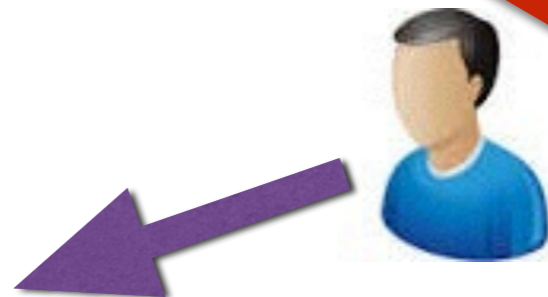
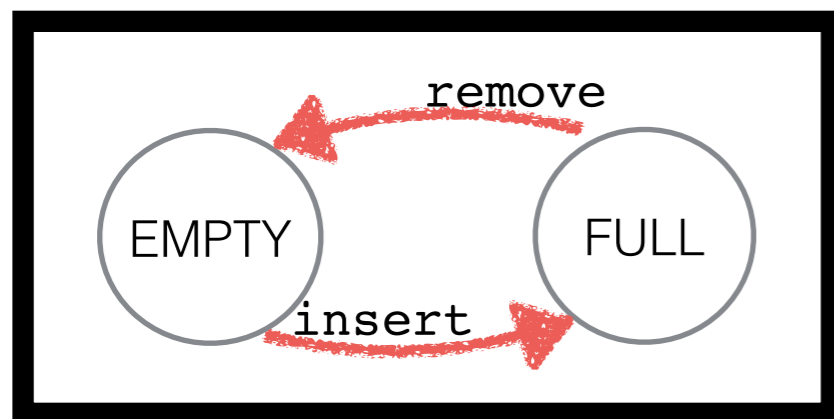


no support from the  
compiler

bad msg!!

~~buffer ! "hello"~~  
buffer ! insert(1)  
buffer ! remove()  
~~buffer ! remove()~~

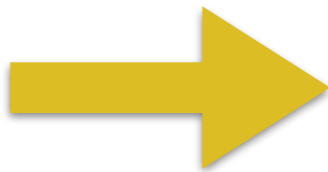
bad state!!



“simpler”  
than Akka Typed

# add a layer of typing

`buffer ! "hello"`  
↓  
has type **ActorRef**,  
which declares  
`def ! (msg: Any)`  
which is *always well-typed*



`buffer ! "hello"` ❌  
↓  
has type **TypedRef[T]**, which

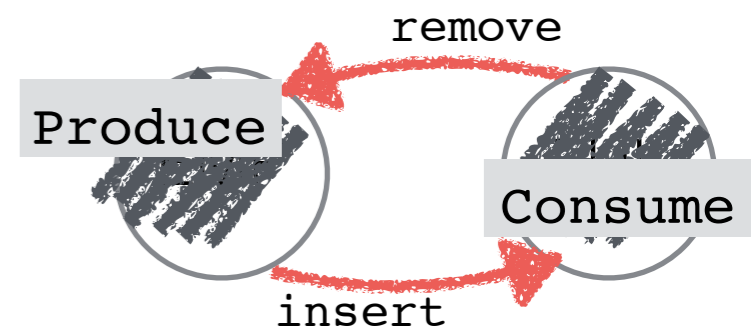
- is a wrapper for an **actor at state T**
- declares `def ! (msg: T)`, hence it **statically type-checks** that only msg belonging to the interface **T** are sent

# add a bit of encapsulation

```
trait BufferInterf
trait Produce extends BufferInterf
trait Consume extends BufferInterf

case class insert[T](value:T) extends Produce
case class remove() extends Consume
```

**Nominal typing:** a Type for each set of allowed messages, i.e. *an Interface for each State*



# 1-place buffer ... *with typed reference*

```
trait BufferInterf
trait Produce extends BufferInterf
trait Consume extends BufferInterf

case class insert[T](value:T) extends Produce
case class remove() extends Consume

class Buffer[T] extends Actor { ...as before... }
```

```
val s = ActorSystem()
val untypedBuffer = s.actorOf(Props(new Buffer[Int]), "buff")
val buffer = new TypedRef[BufferInterf](untypedBuffer)
```

```
val user = s.actorOf(Props(new Actor{
    buffer ! insert(4)    ok
    buffer ! remove()    ok
    buffer ! "hello"     does not compile
}))
```



1. **no other messages** but  
insert and remove



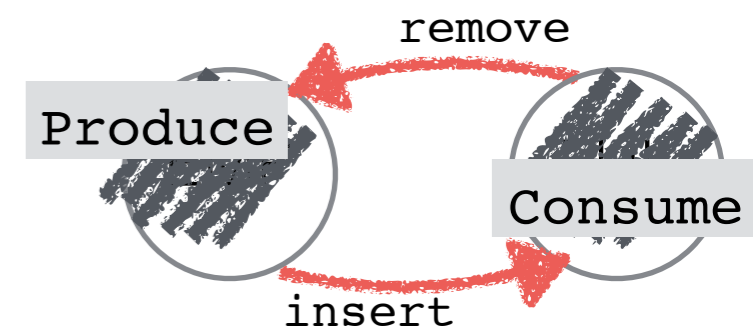
# 1-place buffer ... *with typed reference*

```
val s = ActorSystem()
val untypedBuffer = s.actorOf(Props(new Buffer[Int]), "buff")
val buffer = new TypedRef[Produce](untypedBuffer)

val user = s.actorOf(Props(new Actor{
  buffer ! insert(4)    ok
  buffer ! remove()  does not compile
}))
```



the buffer reference  
**dynamically changes its type**  
between TypedRef[Produce]  
and TypedRef[Consume]



thus at any change we take **a new reference, statically typed with the new type**

**Continuation-passing Style**

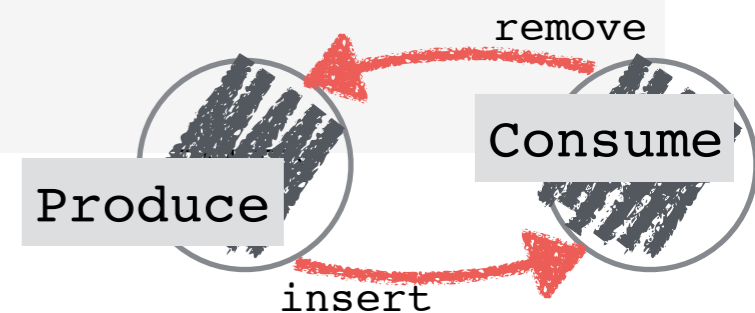
# 1-place buffer *with explicit continuations*

```
case class insert[T](value:T, replyTo:ActorRef) extends Produce
case class remove(replyTo:ActorRef) extends Consume

case class insertReply(o:TypedRef[Consume])
case class removeReply[T](o:TypedRef[Produce])
```

*reply messages  
carry the continuation reference  
with suitable type*

```
class Buffer[T] extends Actor {
  def EMPTY:Receive = {
    case insert(x:T,r) => context.become(FULL(x))
      r ! insertReply(new TypedRef[Consume](self))
  }
  def FULL(x:T):Receive = {
    case remove(r) => context.become(EMPTY)
      r ! removeReply(new TypedRef[Produce](self))
  }
  def receive = EMPTY
}
```



# 1-place buffer *with explicit continuations*

```
case class insert[T](value:T, replyTo:ActorRef) extends Produce
```

```
case class remove(replyTo:ActorRef) extends Consume
```

```
case class insertReply(o:TypedRef[Consume])
```

```
case class removeReply[T](o:TypedRef[Produce])
```

*reply messages  
carry the continuation reference  
with suitable type*

```
val s = ActorSystem()
val untypedBuffer = s.actorOf(Props(new Buffer[Int]), "buff")
val buffer = new TypedRef[Produce](untypedBuffer)

val user = s.actorOf(Props(new Actor{
  buffer ! insert(1, self)
  def run(v:Int) :Receive = {
    case insertReply(o) => o ! remove(self) // insert rises an error
    case removeReply(o) => o ! insert(v+1, self)
                          context.become(run(v+1))
  }
  def receive = run(0)
}))
```

à la  
Akka Typed





# 1-place buffer *with implicit continuations*

```
case class insert(value:Int) extends Produce
case class remove() extends Consume
```

(Typed)  
Monad  
using Futures/  
Promises

```
val s = ActorSystem()
val untypedBuffer = s.actorOf(Props(new Buffer), "buff")
val buffer = new ProtRef[Produce](untypedBuffer, Buffer.protocol)

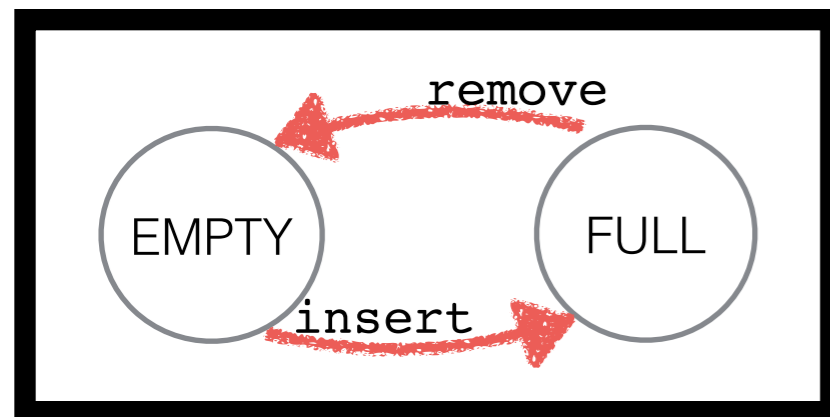
val user = s.actorOf(Props(new Actor{
  for {
    o <- buffer ! insert(1)
    o <- o ! remove()
    o <- o ! insert(2)
    o <- o ! remove()
    o <- o ! insert(3)
    // o ! insert(4) compiler error
    o <- o ! remove()
  } yield print("END")

  def receive= PartialFunction.empty
}))
```



# 1-place buffer as TSOAP

```
class Buffer[T] extends Actor {  
  def EMPTY:Receive = {  
    case insert(x:T) => context.become(FULL(x))  
  }  
  def FULL(x:T):Receive = {  
    case remove() => context.become(EMPTY)  
  }  
  def receive = EMPTY  
}
```



**Producer**



insert(1)  
insert(2)  
insert(3)

...



remove()  
remove()  
remove()

...

**Consumer**

**insert msg can arrive in the buffer's mailbox while the buffer is in state FULL !**

***we still want to ensure that insert / remove are served in the correct state!***

# Chemical semantics *by mixing-in* typed stashing



```
class Buffer[T] extends Actor with Chemical {
  def EMPTY:Receive = chemReact {
    case insert(x:T,r) => chemBecome(FULL(x))
                          r ! insertReply(new TypedRef[Consume](self))
  }
  def FULL(x:T):Receive = chemReact {
    case remove(r) => chemBecome(EMPTY)
                      r ! removeReply(x, new TypedRef[Produce](self))
  }
  def receive = EMPTY
}
```

```
trait ProtocolMsg
```

```
trait Chemical extends Actor with Stash {
  private def check() = { unstashAll() }
  private def keep :Receive = { case (msg:ProtocolMsg,p) => stash() }
  def chemBecome(newState:Receive)={ check(); context.become(newState) }
  def chemReact(behavior:Receive):Receive = behavior orElse keep
}
```

still a clean logic:  
different states with  
different interfaces

```
class Producer(buffer:ProtRef[Produce]) extends Actor {
  for {
    o <- buffer ! insert(0)
    o <- o ! insert(10)
    o <- o ! insert(20)
    o <- o ! insert(30)
    o <- o ! insert(40)
  } yield println("End Producer")
  def receive = PartialFunction.empty
}
```



```
class Consumer(buffer:ProtRef[Consume]) extends Actor{
  for {
    o <- buffer ! remove()
    o <- o ! remove()
    o <- o ! remove()
    o <- o ! remove()
  } yield println("End Consumer")

  def receive = PartialFunction.empty
}
```

```
val s = ActorSystem()
val bufferUntyped = s.actorOf(Props(new Buffer[Int]),"buffer")
val buffer = new ProtocolRef[BufferInterf](bufferUntyped,Buffer.protocol)
val producer1 = s.actorOf(Props(new Producer(buffer,1)))
val consumer1 = s.actorOf(Props(new Consumer(buffer," pippo")))
val consumer2 = s.actorOf(Props(new Consumer(buffer," pluto")))
```

**contravariance**  
of ProtRef[-T]

```

class Producer(buffer:ProtRef[Produce]) extends Actor {
  for {
    o <- buffer ! i
    o <- o ! inse
    o <- o ! inse
    o <- o ! inse
    o <- o ! inse
  } yield println("Er
def receive = Partia
}

```



```

val s = ActorSystem(
val bufferUntyped =
val buffer = new Pro
val producer1 = s.ac
val consumer1 = s.ac
val consumer2 = s.ac

```

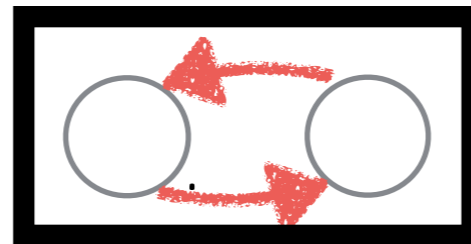
```

produce 1
keeping msg remove(Actor[akka://default/user/$b#-1611031969])
keeping msg remove(Actor[akka://default/user/$c#-1876841699])
inserted 1
removed 1
produce 11
  pippo consumed 1
keeping msg remove(Actor[akka://default/user/$c#-1876841699])
inserted 11
produce 21
removed 11
keeping msg remove(Actor[akka://default/user/$c#-1876841699])
inserted 21
removed 21
  pippo consumed 11
  pluto consumed 21
keeping msg remove(Actor[akka://default/user/$b#-1611031969])
keeping msg remove(Actor[akka://default/user/$c#-1876841699])
produce 31
inserted 31
produce 41
removed 31
  pippo consumed 31
keeping msg remove(Actor[akka://default/user/$c#-1876841699])
inserted 41
removed 41
End Producer n.1
  pippo consumed 41
keeping msg remove(Actor[akka://default/user/$c#-1876841699])
keeping msg remove(Actor[akka://default/user/$b#-1611031969])

```

# what is missing w.r.t. the behavioural typing of Join?

after insert there **must** be a remove



protocols  
expressing **linear**  
**capabilities**



```
insert(1) ; remove ; insert(3) ; remove
```

use the buffer  
**just once**

**Producer**

**Consumer**



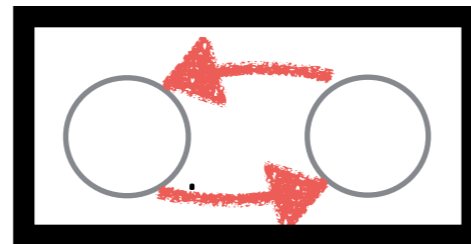
```
insert()  
insert()  
insert()  
...
```



```
remove()  
remove()  
remove()  
...
```

# what is missing w.r.t. the behavioural typing of Join?

after insert there **must** be a remove



```
insert(1) ; remove ; insert(3) ; remove
```

use the buffer **just once**

compliance with protocol **obligations** requires **linear types**

**Producer**

**Consumer**



```
insert()  
insert()  
insert()  
...
```



```
remove()  
remove()  
remove()  
...
```





That's it!

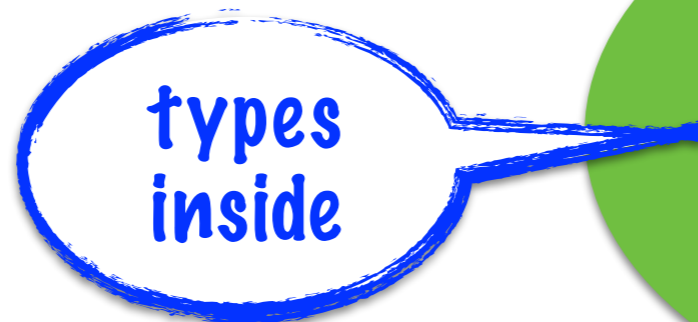
Objective  
Join Calculus

# Protocol-Oriented Distributed Programming

as

TypeState-based

Actor programming



 **Scala**







# Theorem

## Objective Join Calculus



**Formal foundation**

integrating  
the type inference in  
**Scala Akka -compiler**



types  
inside



**merci !**