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## Automi e Linguaggi Formali Homework 3

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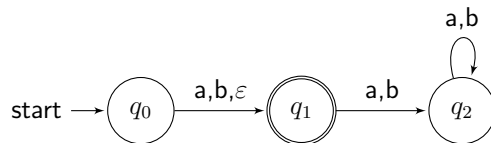
Es.3 Sia  $\mathcal{L}$  il linguaggio definito dalla concatenazione  $\mathcal{L}_1\mathcal{L}_2$  dei seguenti linguaggi sull'alfabeto  $\Sigma^{a,b}$ .

- $L_1 = \{w \mid |w| \leq 1\}$
- $L_2 = \{w \mid \text{ogni posizione dispari in } w \text{ è occupata da un simbolo } b\}$

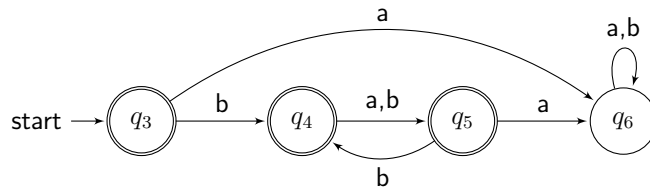
Costruire l'NFA corrispondente e minimizzarlo

**Soluzione:**

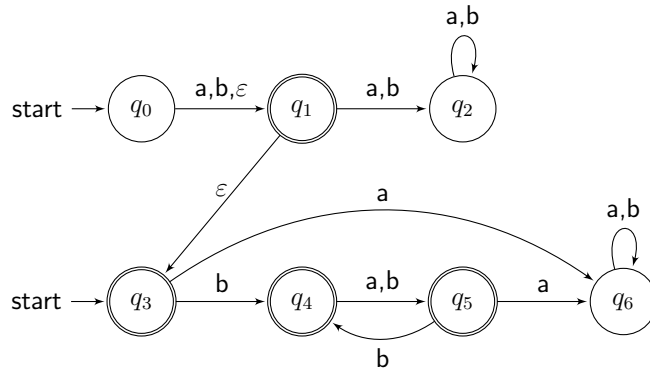
DFA(L1)



DFA(L2)



Concatenazione



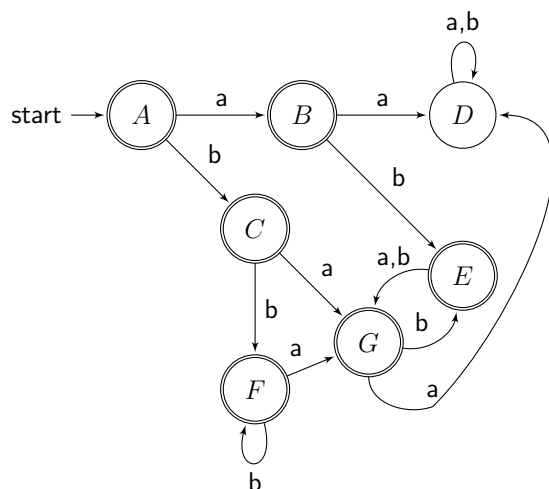
NFA → DFA

Tabella delle transizioni DFA

	a	b
$\vec{*}\{q_0, q_1, q_3\}$	$\{q_1, q_2, q_3, q_6\}$	$\{q_1, q_2, q_3, q_4\}$
$*\{q_1, q_2, q_3, q_6\}$	$\{q_2, q_6\}$	$\{q_2, q_4, q_6\}$
$*\{q_1, q_2, q_3, q_4\}$	$\{q_2, q_5, q_6\}$	$\{q_2, q_4, q_5\}$
$\{q_2, q_6\}$	$\{q_2, q_6\}$	$\{q_2, q_6\}$
$*\{q_2, q_4, q_6\}$	$\{q_2, q_5, q_6\}$	$\{q_2, q_5, q_6\}$
$*\{q_2, q_4, q_5\}$	$\{q_2, q_5, q_6\}$	$\{q_2, q_4, q_5\}$
$*\{q_2, q_5, q_6\}$	$\{q_2, q_6\}$	$\{q_2, q_4, q_6\}$

	a	b
$\vec{*}A$	B	C
$*B$	D	E
$*C$	G	F
D	D	D
$*E$	G	G
$*F$	G	F
$*G$	D	E

DFA



B						
C						
D	X	X	X			
E				X		
F				X		
G				X		
	A	B	C	D	E	F

A, B, C, E, F, G stati finali

<i>B</i>	X					
<i>C</i>		X				
<i>D</i>	X	X	X			
<i>E</i>		X		X		
<i>F</i>		X		X		
<i>G</i>	X		X	X	X	X
	<i>A</i>	<i>B</i>	<i>C</i>	<i>D</i>	<i>E</i>	<i>F</i>

$G, B \neq A, C, E, F$

<i>B</i>	X					
<i>C</i>		X				
<i>D</i>	X	X	X			
<i>E</i>	X	X	X	X		
<i>F</i>		X		X	X	
<i>G</i>	X		X	X	X	X
	<i>A</i>	<i>B</i>	<i>C</i>	<i>D</i>	<i>E</i>	<i>F</i>

$E \neq A, C, F$

DFA minimo

