

$$\sqrt{1 + \frac{\sin x}{2}} > \cos x$$

$$1 + \frac{\sin x}{2} \geq 0 \quad \text{ma} \quad -\frac{1}{2} \leq \frac{\sin x}{2} \leq \frac{1}{2} \quad \text{quindi ok}$$

$$\cos x < 0 \quad \vee \quad \begin{cases} \cos x \geq 0 \\ 1 + \frac{\sin x}{2} > \cos^2 x \end{cases}$$

$$1 + \frac{\sin x}{2} > \frac{1}{2} \geq 0$$

$$\cos x < 0 \quad \text{per} \quad -\frac{\pi}{2} + 2k\pi < x < \frac{\pi}{2} + 2k\pi \quad k \in \mathbb{Z}$$

per risolvere $1 + \frac{\sin x}{2} > \cos^2 x$ si osserva che $\cos^2 x = 1 - \sin^2 x$

Si risolve $\begin{cases} \sin^2 x + \frac{\sin x}{2} > 0 \\ \cos x \geq 0 \end{cases}$

$$\sin x \left(\sin x + \frac{1}{2} \right) > 0$$

Soluzioni

$$2k\pi < x < \frac{11}{6}\pi + 2k\pi$$

$$k \in \mathbb{Z}$$