

# Methods and Models for Combinatorial Optimization

## Course Content

Luigi De Giovanni, Marco Di Summa

Dipartimento di Matematica 'Tullio Levi-Civita', Università di Padova

# Contacts

## Luigi De Giovanni

Dipartimento di Matematica  
office 427

tel. 049 827 1349

luigi@math.unipd.it

## Marco Di Summa

Dipartimento di Matematica  
office 414

tel. 049 827 1348

disumma@math.unipd.it

## Course webpage

<http://www.math.unipd.it/~luigi/courses/metmodoc.html>

# Course goals

- Introduction to advanced modelling and solution techniques for combinatorial optimization problems: selecting among a huge number of alternatives.
- The course aims at providing mathematical and algorithmic tools to solve optimization problems of practical interest, also with the use of the most popular software packages or libraries.
- Relevant applications to / from Data Science:
  - ▶ **Complex network** analysis (e.g social networks, transportation networks)
  - ▶ **Data-Driven optimization** for huge optimization problems (e.g. Air Traffic Flow Management, deterministic approximation of stochastic optimization problems)
  - ▶ **Hybridization** of optimization and learning techniques (e.g. learning promising neighbor solutions)
  - ▶ ...

# MeMoCO: Preliminary Programme (i)

- Review, advanced topics and application of Mathematical Programming and Duality
  - ▶ Linear Programming models, simplex method, basic notions of duality theory
  - ▶ Column generation technique for large size linear programming models
  - ▶ Applications: network flows, production planning optimization, traffic, telecommunication and social networks
- Advanced methods for Mixed **Integer** Linear Programming (MILP)
  - ▶ Alternative formulations, Branch & Bound, Branch & Cut
  - ▶ Applications: TSP, Facility Location, Set Covering etc.

# MeMoCO: Preliminary Programme (ii)

- **Meta-heuristics** for Combinatorial Optimization

- ▶ Neighbourhood search and variants
- ▶ Evolutionary Algorithms
- ▶ Hybridizations (e.g. Matheuristics, learning promising neighbor solutions)

- **Network Optimization**

- ▶ Modelling optimization problems on graphs and flow networks
- ▶ Application to complex network analysis

- **Labs**

- ▶ On-line optimization servers (e.g., NEOS)
- ▶ Optimization software and Algebraic modelling languages (e.g. AMPL, **IBM-OPL**)
- ▶ Optimization libraries (e.g. **IBM Cplex**, Coin-OR, Scip)

# Practical info

## ● **Schedule:**

- ▶ First semester: Thursday, Friday 8:30 - 10:30
- ▶ room 1BC50 **or** LabTA

## ● **Textbooks and course material**

- ▶ Lecture notes provided by the teacher + articles from scientific journals (available **before** the class: read them!)
- ▶ Optimization software packages available on line and in labs
- ▶ <http://www.math.unipd.it/~luigi/courses/metmodoc/metmodoc.html>

## ● **Examination methods**

- ▶ **Two lab exercises:** implementation of 1) a MILP model and 2) a metaheuristic, to be delivered some days before the oral examination.  
Mandatory [1-10 /30, minimum 5]
- ▶ **Oral examination** on course contents.  
Mandatory [1-20 /30, minimum 10].
- ▶ Short project. Optional [+2 to +6 /30] (e.g., after the oral to improve the score if necessary)

# Practical info

- **Schedule:**

- ▶ First semester: Thursday, Friday 8:30 - 10:30
- ▶ room 1BC50 **or** LabTA

- **Textbooks and course material**

- ▶ Lecture notes provided by the teacher + articles from scientific journals (available **before** the class: read them!)
- ▶ Optimization software packages available on line and in labs
- ▶ <http://www.math.unipd.it/~luigi/courses/metmodoc/metmodoc.html>

- **Examination methods**

- ▶ **Two lab exercises:** implementation of 1) a MILP model and 2) a metaheuristic, to be delivered some days before the oral examination.  
Mandatory [1-10 /30, minimum 5]
- ▶ **Oral examination** on course contents.  
Mandatory [1-20 /30, minimum 10].
- ▶ Short project. Optional [+2 to +6 /30] (e.g., after the oral to improve the score if necessary)

# Practical info

## ● **Schedule:**

- ▶ First semester: Thursday, Friday 8:30 - 10:30
- ▶ room 1BC50 **or** LabTA

## ● **Textbooks and course material**

- ▶ Lecture notes provided by the teacher + articles from scientific journals (available **before** the class: read them!)
- ▶ Optimization software packages available on line and in labs
- ▶ <http://www.math.unipd.it/~luigi/courses/metmodoc/metmodoc.html>

## ● **Examination methods**

- ▶ **Two lab exercises:** implementation of 1) a MILP model and 2) a metaheuristic, to be delivered some days before the oral examination.  
Mandatory [1-10 /30, minimum 5]
- ▶ **Oral examination** on course contents.  
Mandatory [1-20 /30, minimum 10].
- ▶ Short project. Optional [+2 to +6 /30] (e.g., after the oral to improve the score if necessary)