Interactive Computing with MATLAB

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Starting MATLAB

- Double click on the MATLAB icon, or on unix systems type "matlab" at the command line.
- After startup MATLAB displays a *command window* that is used to enter commands and display text-only results.
- Enter Commands at the command prompt:
 - >> for full versionEDU> for educational version
- MATLAB responds to commands by printing text in the command window, or by opening a *figure window* for graphical output.
- Toggle between windows by clicking on them with the mouse.

MATLAB as a Calculator (1)

Enter formulas at the command prompt

>> 2 + 6 - 4 (press return after "4")
ans =
 4
>> ans/2
ans =
 2

MATLAB as a Calculator (2)

Define and use variables

Built-in Variables

pi $(=\pi)$ and ans are a built-in variables

Note: There is no "degrees" mode. All angles are measured in radians.

Built-in Functions

Many standard mathematical functions, such as sin, cos, log, and log10, are built-in

>> log(256) log(x) computes the natural logarithm of x
ans =
5.5452
>> log10(256) log10(x) is the base 10 logarithm
ans =
2.4082
>> log2(256) log2(x) is the base 2 logarithm
ans =
8

Ways to Get Help

• Use on-line help to request info on a specific function

>> help sqrt

• In MATLAB version 6 and later the doc function opens the on-line version of the manual. This is very helpful for more complex commands.

>> doc plot

- Use lookfor to find functions by keywords
 - >> lookfor functionName

On-line Help (1)

Syntax:

help functionName

Example:

>> help log

produces

LOG Natural logarithm. LOG(X) is the natural logarithm of the elements of X. Complex results are produced if X is not positive.

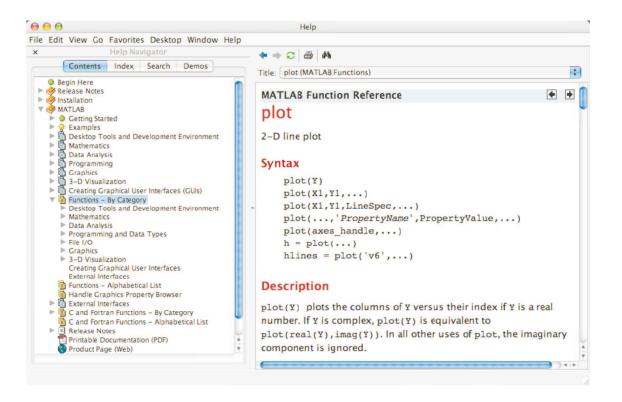
See also LOG2, LOG10, EXP, LOGM.

The help function provides a compact summary of how to use a command. Use the doc function to get more in-depth information.

On-line Help (2)

The help browser opens when you type a doc command:

>> doc plot



Looking for Functions

Syntax:

lookfor string

searches first line of function descriptions for "string".

Example:

>> lookfor cosine

produces

- ACOS Inverse cosine. ACOSH Inverse hyperbolic cosine. COS Cosine.
- COSH Hyperbolic cosine.

Strategies for Interactive Computing

- Use the command window for short sequences of calculations
- Later we'll learn how to build reusable functions for more complex tasks.
- The command window is good for testing ideas and running sequences of operations contained in functions
- Any command executed in the command window can also be used in a function.

Let's continue with a tour of interactive computing.

Suppress Output with Semicolon (1)

Results of intermediate steps can be suppressed with semicolons.

Example: Assign values to x, y, and z, but only display the value of z in the command window:

Suppress Output with Semicolon (2)

Type variable name and omit the semicolon to print the value of a variable (that is already defined)

Multiple Statements per Line

Use commas or semicolons to enter more than one statement at once. Commas allow multiple statements per line without suppressing output.

```
>> a = 5; b = sin(a), c = cosh(a)
b =
        -0.9589
c =
        74.2099
```

MATLAB Variables Names

Legal variable names:

- Begin with one of a-z or A-Z
- Have remaining characters chosen from a–z, A–Z, 0–9, or $_$
- Have a maximum length of 31 characters
- Should not be the name of a built-in variable, built-in function, or user-defined function

Examples:

xxxxxxxx pipeRadius widgets_per_box mySum mysum **Note:** mySum and mysum are *different* variables. MATLAB is *case sensitive*.

Built-in MATLAB Variables (1)

| Name | Meaning |
|---------|---------------------------------------------------------------------------|
| ans | value of an expression when that expression is not assigned to a variable |
| eps | floating point precision |
| pi | π , (3.141492) |
| realmax | largest positive floating point number |
| realmin | smallest positive floating point number |
| Inf | ∞ , a number larger than realmax, the result of evaluating $1/0$. |
| NaN | not a number, the result of evaluating $0/0$ |

Built-in MATLAB Variables (2)

Rule: Only use built-in variables on the right hand side of an expression. Reassigning the value of a built-in variable can create problems with built-in functions.

Exception: i and j are preassigned to $\sqrt{-1}$. One or both of i or j are often reassigned as loop indices. More on this later.

Matrices and Vectors

All MATLAB variables are matrices

- A vector is a matrix with one row *or* one column.
- A scalar is a matrix with one row *and* one column.
- A character string is a row of column vector of characters.

Consequences:

- Rules of linear algebra apply to addition, subtraction and multiplication.
- Elements in the vectors and matrices are addressed with Fortran-like subscript notation, e.g.,, x(2), A(4,5). Usually this notation is clear from context, but it can be confused with a function call,

| y = sqrt(5) | sqrt is a built-in function |
|-------------|------------------------------|
| z = f(3) | Is f a function or variable? |

Creating MATLAB Variables

 Matlab variables are created with an assignment statement

>> x = expression

where *expression* is a legal combinations of numerical values, mathematical operators, variables, and function calls.

The *expression* can involve:

- Manual entry
- Built-in functions that return matrices
- Custom (user-written) functions that return matrices
- Loading matrices from text files or "mat" files

Element-by-Element Creation of Matrices and Vectors (1)

A matrix, a column vector, and a row vector: As MATLAB variables: >> A = [3 2; 3 1; 1

Element-by-Element Creation of Matrices and Vectors (2)

For manual entry, the elements in a vector are enclosed in square brackets. When creating a row vector, separate elements with a space.

Separate columns with a semicolon

Element-by-Element Creation of Matrices and Vectors (3)

When assigning elements to matrix, row elements are separated by spaces, and columns are separated by semicolons

>> A = [1 2 3; 5 7 11; 13 17 19] A = 1 2 3 5 7 11 13 17 19

Transpose Operator (1)

Once it is created, a variable can be transformed with other operators. The *transpose operator* converts a row vector to a column vector (and *vice versa*), and it changes the rows of a matrix to columns.

```
>> v = [2 4 1 7]
v =
2 4 1 7
>> w = v'
w =
2
4
1
7
```

Transpose Operator (2)

>> A = [1 2 3; 4 5 6; 7 8 9] A = З 5 6 >> B = A' В =

Overwriting Variables

Once a variable has been created, it can be reassigned

```
>> x = 2;
>> x = x + 2
x =
   4
>> y = [1 2 3 4]
y =
      2
               3
    1
                     4
>> y = y'
y =
    1
    2
    3
    4
```

Using Functions to Create Matrices and Vectors

Create vectors with built-in functions:

linspace and logspace

Create matrices with built-in functions:

```
ones, zeros, eye, diag, ...
```

Note that ones and zeros can also be used to create vectors.

Creating vectors with linspace (1)

The linspace function creates vectors with elements having uniform linear spacing.

Syntax:

x = linspace(startValue,endValue)
x = linspace(startValue,endValue,nelements)

Examples:

```
>> u = linspace(0.0,0.25,5)
u =
0 0.0625 0.1250 0.1875 0.2500
```

```
>> u = linspace(0.0,0.25);
```

Remember: Ending a statement with semicolon suppresses the output.

Creating vectors with linspace (2)

Column vectors are created by appending the transpose operator to linspace

```
>> v = linspace(0,9,4)'
v =
0
3
6
9
```

Example: A Table of Trig Functions

```
>> x = linspace(0,2*pi,6)';
                         (note transpose)
>> y = sin(x);
>> z = cos(x);
>> [x y z]
ans =
        0
                 0
                   1.0000
   1.2566 0.9511 0.3090
   2.5133 0.5878 -0.8090
   3.7699 -0.5878 -0.8090
   5.0265 -0.9511 0.3090
   6.2832
                      1.0000
                 0
```

The expressions y = sin(x) and z = cos(x) take advantage of *vectorization*. If the input to a vectorized function is a vector or matrix, the output is often a vector or matrix having the same shape. More on this later.

Functions to Create Matrices (2)

Use ones and zeros to set intial values of a matrix or vector.

Syntax:

- A = ones(nrows,ncols)
- A = zeros(nrows,ncols)

Examples:

```
>> D = ones(3,3)
D =
    1
        1
              1
    1
      1
              1
    1
         1
              1
>> E = ones(2,4)
E =
    1
         1 1
                   1
              1
    1
         1
                   1
```

Functions to Create Matrices (3)

ones and zeros are also used to create vectors. To do so, set either *nrows* or *ncols* to 1.

Functions to Create Matrices (4)

The eye function creates identity matrices of a specified size. It can also create non-square matrices with ones on the main diagonal.

Syntax:

Examples:

```
>> C = eye(5)
C =
     1
           0
                 0
                        0
                              0
     0
           1
                 0
                              0
                        0
                  1
     0
           0
                        0
                              0
     0
                 0
                        1
                              0
           0
                              1
     0
           0
                  0
                        0
```

Functions to Create Matrices (5)

The optional second input argument to eye allows non-square matrices to be created.

>> D = eye(3,5) D = 1 0 0 0 0 0 1 0 0 0 0 1 0 0

where $D_{i,j} = 1$ whenever i = j.

Functions to Create Matrices (6)

The **diag** function can *either* create a matrix with specified diagonal elements, *or* extract the diagonal elements from a matrix

Syntax:

A = diag(v)v = diag(A)

Example: Use diag to create a matrix

Functions to Create Matrices (7)

Example: Use diag to extract the diagonal of a matrix

>> B = [1:4; 5:8; 9:12] B = >> w = diag(B)w =

Functions to Create Matrices (8)

The action of the diag function depends on the characteristics and number of the input(s). This polymorphic behavior of MATLAB functions is common. Refer to the on-line documentation for the possible variations.

```
>> A = diag([3 2 1])
                                Create a matrix with a specified diagonal
A =
     3
            0
                  0
            2
     0
                  0
     0
            0
                  1
>> B = [4 2 2; 3 6 9; 1 1 7];
>> v = diag(B)
                                   Extract the diagonal of a matrix
v =
     4
     6
     7
```

Subscript Notation (1)

If A is a matrix, A(i,j) selects the element in the ith row and jth column. Subscript notation can be used on the right hand side of an expression to refer to a matrix element.

Subscript Notation (1)

Subscript notation is also used to assign matrix elements

Referring to elements beyond the dimensions the matrix results in an error

>> A = [1 2 3; 4 5 6; 7 8 9];
>> A(1,4)
??? Index exceeds matrix dimensions.

Subscript Notation (1)

Assigning an element that is beyond the existing dimensions of the matrix causes the matrix to be resized!

```
>> A = [1 2 3; 4 5 6; 7 8 9];
A =
    1
        2
             3
         5 6
    4
    7
         8
             9
>> A(4,4) = 11
A =
    1
        2
             3
                  0
    4
         5 6
                  0
    7
             9
         8
                  0
    0
         0
             0
                  11
```

In other words, MATLAB automatically resizes matrices on the fly.

Colon Notation (1)

Colon notation is very powerful and very important in the effective use of $\rm MATLAB.$ The colon is used as both an operator and as a wildcard.

Use colon notation to:

- create vectors
- refer to or extract ranges of matrix elements

Colon Notation (2)

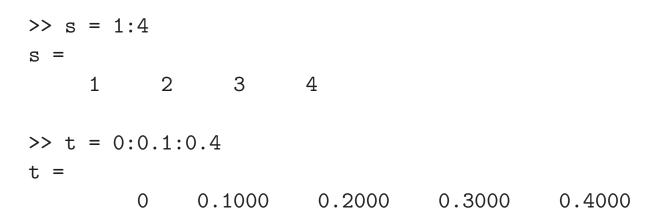
Syntax:

startValue:endValue
startValue:increment:endValue

Note: *startValue*, *increment*, and *endValue* do not need to be integers

Colon Notation (3)

Creating row vectors:



Colon Notation (4)

Creating column vectors:

>> u = (1:5)'
u =
 1
 2
 3
 4
 5
>> v = 1:5'
v =
 1 2 3 4 5
v is a row vector because 1:5' creates a vector between 1 and the
transpose of 5.

Colon Notation (5)

Use colon as a wildcard to refer to an entire column or row

Colon Notation (6)

Or use colon notation to refer to subsets of columns or rows

Colon Notation (7)

Colon notation is often used in compact expressions to obtain results that would otherwise require several steps.

Example:

| >> A = ones(8,8); >> A(3:6,3:6) = zeros(4,4) | | | | | | | | |
|-------------------------------------------------|---|---|---|---|---|---|---|---|
| A = | | | | | | | | |
| | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| | 1 | 1 | 0 | 0 | 0 | 0 | 1 | 1 |
| | 1 | 1 | 0 | 0 | 0 | 0 | 1 | 1 |
| | 1 | 1 | 0 | 0 | 0 | 0 | 1 | 1 |
| | 1 | 1 | 0 | 0 | 0 | 0 | 1 | 1 |
| | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |

Colon Notation (8)

Finally, colon notation is used to convert any vector or matrix to a column vector.

Example:

Colon Notation (9)

Colon notation converts a matrix to a column vector by appending the columns of the input matrix

Note: The **rand** function generates random elements between zero and one. Repeating the preceding statements will, in all likelihood, produce different numerical values for the elements of v.

A Quick Overview of Linear Algebra in MATLAB

The name "MATLAB" is a shortened form of "MATrix LABoratory".

MATLAB data types and syntax make it easy to perform standard operations of linear algebra including addition, subtraction, and multiplication of vectors and matrices.

Chapter 7 provides a detailed review of linear algebra. Here we provide a simple introduction to some operations that are necessary for routine calculation.

- Vector addition and subtraction
- Inner and outer products
- Vectorization
- Array operators

Vector Addition and Subtraction

Vector and addition and subtraction are element-by-element operations.

Example:

```
>> u = [10 9 8]; (u and v are row vectors)
>> v = [1 2 3];
>> u+v
ans =
    11   11   11
>> u-v
ans =
    9   7   5
```

Vector Inner and Outer Products

The inner product combines two vectors to form a scalar

$$\sigma = u \cdot v = u \, v^T \Longleftrightarrow \sigma = \sum u_i \, v_i$$

The outer product combines two vectors to form a matrix

$$A = u^T v \Longleftrightarrow a_{i,j} = u_i v_j$$

Inner and Outer Products in MATLAB

Inner and outer products are supported in ${\rm MATLAB}$ as natural extensions of the multiplication operator

| >> u = [2 | 10 9 8 |]; | (u and v are row vectors) |
|-----------|--------|----|---------------------------|
| >> v = [: | L 2 3] | • | |
| >> u*v' | | | (inner product) |
| ans = | | | |
| 52 | | | |
| | | | |
| >> u'*v | | | (outer product) |
| ans = | | | |
| 10 | 20 | 30 | |
| 9 | 18 | 27 | |
| 8 | 16 | 24 | |
| | | | |

Vectorization

- Vectorization is the use of single, compact expressions that operate on all elements of a vector without explicitly writing the code for a loop. The loop *is* executed by the MATLAB kernel, which is much more efficient at evaluating a loop in interpreted MATLAB code.
- Vectorization allows calculations to be expressed succintly so that programmers get a high level (as opposed to detailed) view of the operations being performed.
- Vectorization is important to make MATLAB operate efficiently².

²Recent versions of MATLAB have improved the efficiency for some non-vectorized code.

Vectorization of Built-in Functions

Most built-in function support *vectorized* operations. If the input is a scalar the result is a scalar. If the input is a vector or matrix, the output is a vector or matrix with the same number of rows and columns as the input.

Example:

| >> x | = 0:pi/4 | 4:pi | (define a row vector) | | | |
|------|-------------|--------|-----------------------|--------------|---------------|--|
| x = | 0 | 0.7854 | 1.5708 | 2.3562 | 3.1416 | |
| Ū | $= \cos(x)$ |) | (eval | luate cosine | of each x(i)) | |
| y = | 1.0000 | 0.7071 | 0 | -0.7071 | -1.0000 | |

Contrast with FORTRAN Implementation

The Matlab statements

```
x = 0:pi/4:pi;
y = cos(x);
```

are equivalent to the following FORTRAN code

```
real x(5),y(5)
pi = 3.14159624
dx = pi/4.0
do 10 i=1,5
    x(i) = (i-1)*dx
    y(i) = sin(x(i))
```

10 continue

No explicit loop is necessary in MATLAB

Vectorized Calculations (6)

More examples

| >> A = pi*[1 2; 3 4] | >> B = A/2 | | |
|-----------------------|---------------|--|--|
| A = | B = | | |
| 3.1416 6.2832 | 1.5708 3.1416 | | |
| 9.4248 12.5664 | 4.7124 6.2832 | | |
| >> S = sin(A) | >> T = sin(B) | | |
| S = | T = | | |
| 0 0 | 1 0 | | |
| 0 0 | -1 0 | | |

Array Operators

Array operators support element-by-element operations that are not defined by the rules of linear algebra.

Array operators have a period prepended to a standard operator.

| Symbol | Operation |
|--------|-------------------------------------|
| .* | element-by-element multiplication |
| ./ | element-by-element "right" division |
| .\ | element-by-element "left" division |
| .^ | element-by-element exponentiation |

Array operators are a very important tool for writing vectorized code.

Using Array Operators (1)

Examples: Element-by-element multiplication and division

>> u = [1 2 3]; >> v = [4 5 6];

Use .* and ./ for element-by-element multiplication and division

Using Array Operators (1)

Examples: Element-by-element multiplication and division

Using Array Operators (2)

Examples: Application to matrices

The last statement causes an error because the number of columns in A is not equal to the number of rows in B - a requirement for A and B to be compatible for matrix multiplication.

Using Array Operators (3)

The number of columns in A is equal to the number of rows in B^T , so A*B' is a legal matrix-matrix multiplication.

Array operators also apply to matrix powers.

>> A.² ans = 1 4 9 16 25 36 49 64

Plotting

- Plotting (x, y) data
- Axis scaling and annotation
- 2D (contour) and 3D (surface) plotting

Plotting (x,y) Data (1)

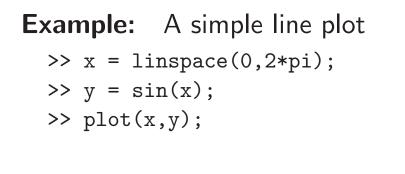
Two dimensional plots are created with the **plot** function

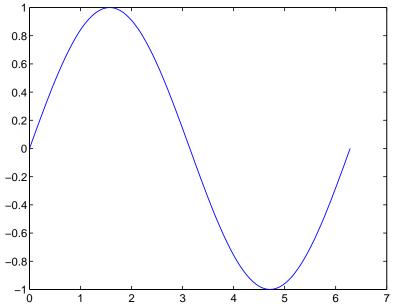
Syntax:

```
plot(x,y)
plot(xdata,ydata,symbol)
plot(x1,y1,x2,y2,...)
plot(x1,y1,symbol1,x2,y2,symbol2,...)
```

Note: x and y must have the same *shape*, x1 and y1 must have the same *shape*, x2 and y2 must have the same *shape*, etc.

Plotting (x, y) Data (2)





Line and Symbol Types (1)

The curves for a data set are drawn from combinations of the color, symbol, and line types in the following table.

| Color | | Symbols | | | Line | | |
|-------|---------|---------|--------------------|---|------------------|---|---------|
| У | yellow | • | point | ^ | triangle (up) | - | solid |
| m | magenta | 0 | circle | < | triangle (left) | : | dotted |
| С | cyan | x | x-mark | > | triangle (right) | | dashdot |
| r | red | + | plus | р | pentagram | | dashed |
| g | green | * | star | h | hexagram | | |
| b | blue | S | square | | | | |
| W | white | d | diamond | | | | |
| k | black | V | triangle (down) | | | | |

To choose a color/symbol/line style, chose one entry from each column.

Line and Symbol Types (2)

Examples:

Put yellow circles at the data points:

```
plot(x,y,'yo')
```

Plot a red dashed line with no symbols:

```
plot(x,y,'r--')
```

Put black diamonds at each data point and connect the diamonds with black dashed lines:

plot(x,y,'kd--')

Alternative Axis Scaling (1)

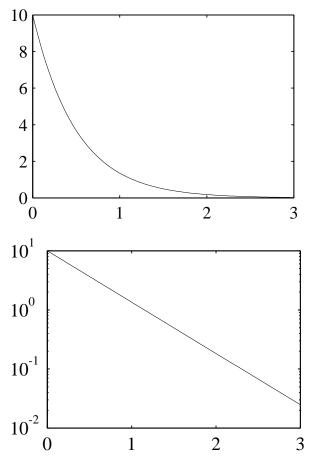
Combinations of linear and logarithmic scaling are obtained with functions that, other than their name, have the same syntax as the **plot** function.

| Name | Axis scaling |
|----------|--------------------------------------|
| loglog | $\log_{10}(y)$ versus $\log_{10}(x)$ |
| plot | linear y versus x |
| semilogx | linear y versus $\log_{10}(x)$ |
| semilogy | $\log_{10}(y)$ versus linear x |

Note: As expected, use of logarithmic axis scaling for data sets with negative or zero values results in a error. MATLAB will complain and then plot only the positive (nonzero) data.

Alternative Axis Scaling (2)

Example: >> x = linspace(0,3); >> y = $10 \exp(-2 x)$; >> plot(x,y); >> semilogy(x,y);



Multiple plots per figure window (1)

The **subplot** function is used to create a matrix of plots in a single figure window.

Syntax:

```
subplot(nrows,ncols,thisPlot)
```

Repeat the values of *nrows* and *ncols* for all plots in a single figure window. Increment *thisPlot* for each plot

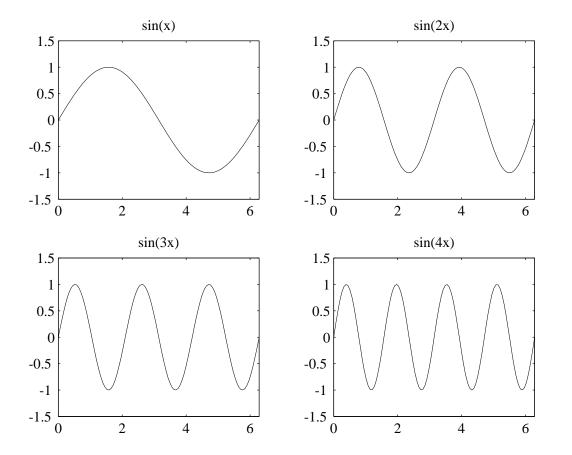
Multiple plots per figure window (1)

Example:

```
>> x = linspace(0,2*pi);
>> subplot(2,2,1);
>> plot(x,sin(x)); axis([0 2*pi -1.5 1.5]); title('sin(x)');
>> subplot(2,2,2);
>> plot(x,sin(2*x)); axis([0 2*pi -1.5 1.5]); title('sin(2x)');
>> subplot(2,2,3);
>> plot(x,sin(3*x)); axis([0 2*pi -1.5 1.5]); title('sin(3x)');
>> subplot(2,2,4);
>> plot(x,sin(4*x)); axis([0 2*pi -1.5 1.5]); title('sin(4x)');
```

(See next slide for the plot.)

Multiple plots per figure window (2)



Plot Annotation

| Name | Operation(s) performed |
|--------|----------------------------------------------------------------------------------------------------|
| axis | Reset axis limits |
| grid | Draw grid lines at the major ticks marks on the x and y axes |
| gtext | Add text to a location determined by a mouse click |
| legend | Create a legend to identify symbols and line types when multiple curves are drawn on the same plot |
| text | Add text to a specified (x, y) location |
| xlabel | Label the <i>x</i> -axis |
| ylabel | Label the y -axis |
| title | Add a title above the plot |