4.a Fixed-Priority Scheduling

Credits to A. Burns and A. Wellings

Simple workload model

- The application is assumed to consist of a fixed set of tasks
- All tasks are *periodic* with known periods
 This defines the *periodic workload model*
- The tasks are completely *independent* of each other
- All system overheads (context-switch times, interrupt handling and so on) are ignored
 - □ Assumed to have zero cost or otherwise negligible
- All tasks have a deadline equal to their period (D = T)
 Each task must complete before it is next released
- All tasks have a fixed WCET (a safe and tight upper-bound)

Operation modes are not considered

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Standard notation

- B: Worst-case blocking time for the task (if applicable)
- *C*: Worst-case computation time (WCET) of the task
- D: Deadline of the task
- *I*: The interference time of the task
- J: Release jitter of the task
- *N*: Number of tasks in the system
- P: Priority assigned to the task (if applicable)
- R: Worst-case response time of the task
- T: Minimum time between task releases (or task period)
- U: The utilization of each task (equal to C/T)
- a-Z: The name of a task

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| Fixed-priority scheduling (FPS)

- At present the most widely used approach
 - □ The distinct focus of this segment
- Each task has a fixed (static) priority computed off-line
- The ready tasks are dispatched to execution in the order determined by their priority
- In real-time systems the "priority" of a task is derived from its temporal requirements, not its importance to the correct functioning of the system or its integrity



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Preemption and non-preemption /1

- With priority-based scheduling, a high-priority task may be released during the execution of a lower priority one
- In a *preemptive* scheme, there will be an immediate switch to the higher-priority task
- With *non-preemption*, the lower-priority task will be allowed to complete before the other may execute
- Preemptive schemes enable higher-priority tasks to be more reactive, hence they are preferred

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Preemption and non-preemption /2

- Alternative strategies allow a lower priority task to continue to execute for a bounded time
- These schemes are known as deferred preemption or cooperative dispatching
- Schemes such as EDF can also take on a preemptive or non-preemptive form
- Value-based scheduling (VBS) can too
 - □ VBS is useful when the system becomes overloaded and some *adaptive* scheme of scheduling is needed
 - VBS consists in assigning a value to each task and then employing an on-line value-based scheduling algorithm to decide which task to run next

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Rate-monotonic priority assignment

- Each task is assigned a (unique) priority based on its period
 - □ The shorter the period, the higher the priority
 - □ Tasks are assigned distinct priorities (!)
- For any two tasks τ_i , τ_i we have $T_i < T_i \rightarrow P_i > P_i$
 - Rate monotonic assignment is optimal under preemptive priority-based scheduling

■ Nomenclature

□ Priority 1 as numerical value is the lowest (least) priority but the indices are still sorted highest to lowest (!)

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Utilization-based analysis

- A simple *schedulability test* (thus sufficient but not necessary) exists for rate monotonic scheduling
 - \Box But only for task sets with D = T

$$U = \sum_{i=1}^{N} \frac{C_i}{T_i} \le N (2^{1/N} - 1)$$

 $U \le 0.69$ as $N \to \infty$

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Example: task set A

Task	Period	Computation Time	Priority	Utilization
	T	С	P	U
a	50	12	1 (low)	0.24
b	40	10	2	0.25
С	30	10	3 (high)	0.33

- The combined utilization is 0.82 (or 82%)
- This is above the threshold for three tasks (0.78), hence this task set fails the utilization test
- Then we have no a-priori answer

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Example: task set B

Task	Period	Computation Time	Priority	Utilization
	Т	С	P	U
a	80	32	1 (low)	0.40
b	40	5	2	0.125
С	16	4	3 (high)	0.25

- The combined utilization is 0.775
- This is below the threshold for three tasks (0.78), hence this task set will meet all its deadlines

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Timeline for task set A Task Task Release Time a Deadline Met b Task Completion Time Deadline Missed Preempted Executing 20 50 10 60 Time -2014/15 UniPD / T. Vardanega Real-Time Systems 169 of 492

| Example: task set C

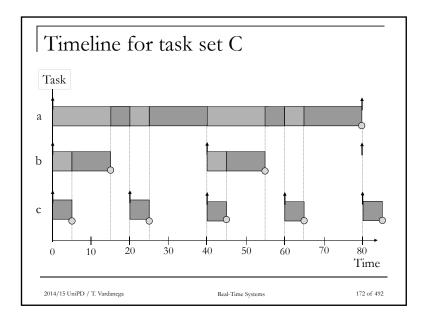
Task	Period	Computation Time	Priority	Utilization
	Т	С	P	U
a	80	40	1 (low)	0.50
b	40	10	2	0.25
С	20	5	3 (high)	0.25

- The combined utilization is 1.0
- This is above the threshold for three tasks (0.78) but the task set will meet all its deadlines (!)

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Critique of utilization-based tests

- They are not exact
- They are not general
- But they are \(\Omega(N)\)□ Which makes them interesting for a large class of users
- The test is said to be sufficient but not necessary and as such falls in the class of *schedulability tests*

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Response time analysis /1

■ The worst-case response time R_i of task τ_i is first calculated and then checked (trivially) with its deadline

$$R_i \leq D_i$$

$$R_i = C_i + I_i$$

 \Box Where *I* is the interference from higher-priority tasks

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Calculating R

- Within R_i , each higher priority task τ_j will execute a $\left[\frac{R_i}{T_i}\right]$ times
 - \Box The ceiling function [f] gives the smallest integer greater than the fractional number f on which it acts
 - E.g., the ceiling of 1/3 is 1, of 6/5 is 2, and of 6/3 is 2
- The total interference suffered by τ_i from τ_j in R_i is given by $\left[\frac{R_i}{T_i}\right]C_j$

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Response time equation

$$R_{i} = C_{i} + \sum_{j \in hp(i)} \left\lceil \frac{R_{i}}{T_{j}} \right\rceil C_{j}$$

- Where hp(i) is the set of tasks with priority higher than task τ_i
- Solved by forming a recurrence relationship

$$w_i^{n+1} = C_i + \sum_{j \in hp(i)} \left[\frac{w_i^n}{T_i} \right] C_j$$

- The set of values $w_i^0, w_i^1, w_i^2, ..., w_i^n$,... is monotonically non-decreasing
- When $w_i^n = w_i^{n+1}$ the solution to the equation has been found
- w_i^0 must not be greater than C_i (e.g. 0 or C_i)

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Example: task set D

Task	Period	Computation Time	Priority	Utilization
	Т	С	P	U
a	7	3	3 (high)	0.4285
b	12	3	2	0.25
с	20	5	1 (low)	0.25

$$\begin{bmatrix}
R_a = 3
\end{bmatrix}$$

$$\begin{cases}
w_b^1 = 3 \\
w_b^1 = 3 + \left\lceil \frac{3}{7} \right\rceil 3 = 6
\end{cases}$$

$$\begin{cases}
w_b^2 = 3 + \left\lceil \frac{6}{7} \right\rceil 3 = 6
\end{cases}$$

$$\begin{bmatrix}
R_b = 6
\end{bmatrix}$$

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Response time algorithm

```
for i in 1..N loop -- for each task in turn
  n := 0
   w^n := C
100p
                                       If the recurrence does not converge
      calculate new w_i^{n+1}
                                       before T; we can still set a termination
     if w_i^{n+1} = w_i^n then
                                       condition that attempts to determine
        R_i = w_i^n
                                       how long past T<sub>i</sub> job i completes
        exit value found
      end if
     if w_{i}^{n+1} > T_{i} then
        exit value not found
     end if
     n := n + 1
   end loop
end loop
```

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| Example (cont'd)

$$w_{c}^{1} = 5 + \left\lceil \frac{5}{7} \right\rceil 3 + \left\lceil \frac{5}{12} \right\rceil 3 = 11$$

$$w_{c}^{2} = 5 + \left\lceil \frac{11}{7} \right\rceil 3 + \left\lceil \frac{11}{12} \right\rceil 3 = 14$$

$$w_{c}^{3} = 5 + \left\lceil \frac{14}{7} \right\rceil 3 + \left\lceil \frac{14}{12} \right\rceil 3 = 17$$

$$w_{c}^{4} = 5 + \left\lceil \frac{17}{7} \right\rceil 3 + \left\lceil \frac{17}{12} \right\rceil 3 = 20$$

$$w_{c}^{5} = 5 + \left\lceil \frac{20}{7} \right\rceil 3 + \left\lceil \frac{20}{12} \right\rceil 3 = 20$$

$$R_{c} = 20$$

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Revisiting task set C

Task	Period	Computation Time	Priority	Response Time
	Т	С	P	R
a	80	40	1 (low)	80
b	40	10	2	15
с	20	5	3 (high)	5

- The combined utilization is 1.0
- This is above the utilization threshold for three tasks (0.78) hence the utilization-based schedulability test failed
- But RTA shows that the task set will meet all its deadlines (cf. the impasse we had at page 169)

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Response time analysis /2

- RTA is a feasibility test
 - □ Thus exact, hence necessary and sufficient
- If the task set passes the test then all its tasks will meet all their deadlines
- If it fails the test then, at run time, some tasks will miss their deadline and FPS tells us exactly which
 - □ Unless the computation time estimations (the WCET) themselves turn out to be pessimistic

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| Sporadic tasks

- Sporadic tasks have a *minimum inter-arrival time*
 - Which should be preserved at run time if schedulability is to be ensured, but how can it?
- They also require $D \le T$
- The RTA for FPS works perfectly for D<T as long as the stopping criterion becomes

$$W_i^{n+1} > D_i$$

■ Interestingly this also works perfectly well with *any* priority ordering

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Hard and soft tasks

- In many situations the WCET given for sporadic tasks are considerably higher than the average case
- Interrupts often arrive in bursts and an abnormal sensor reading may lead to significant additional computation
- Measuring schedulability with WCET may lead to very low processor utilizations being observed in the actual running system
 - $\ensuremath{\square}$ We need some common sense to contain pessimism

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General common-sense guidelines

- Rule 1: All tasks (hard and soft) should be schedulable using average execution times and average arrival rates for both periodic and sporadic tasks
 - □ There may therefore be situations in which it is not possible to meet all current deadlines
 - ☐ This condition is known as a transient overload
- Rule 2: All hard real-time tasks should be schedulable using WCET and worst-case arrival rates of all tasks (including soft)
 - □ No hard real-time task will therefore miss its deadline
 - ☐ If Rule 2 incurs unacceptably low utilizations for non-worst-case jobs then WCET values or arrival rates must be reduced

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| Handing aperiodic tasks /1

- These do not have minimum inter-arrival times
 - And consequently also no deadline
 - □ However we may be interested in the system being responsive to them
- We can run aperiodic tasks at a priority below the priorities assigned to hard tasks
 - In a preemptive system they therefore cannot steal resources from the hard tasks
- But this does not provide adequate support to soft tasks which will often miss their deadlines
- To improve the situation for soft tasks, a server can be employed
- Servers protect the processing resources needed by hard tasks but otherwise allow soft tasks to run as soon as possible

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Handing aperiodic tasks /2

- Besides preserving hard tasks and giving fair opportunities to soft tasks we still would like to schedule aperiodic jobs in a manner that minimizes
 - □ The response time of the job at the head of the aperiodic job queue
 - Or else the average response time of all aperiodic jobs for a given queuing discipline
- Possible solutions
 - □ Execute the aperiodic jobs in the background
 - Execute the aperiodic jobs by interrupting the periodic jobs



Slack stealing

Use dedicated servers



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| Handing aperiodic tasks /3

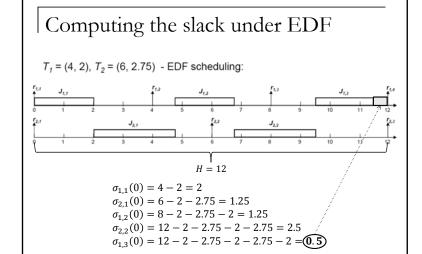
■ Slack stealing

- \Box Difficult for preemptive systems because, for them, the slack $\sigma(t)$ is a function of the time t at which it is computed
- □ The slack stealer is ready when the aperiodic queue is not empty and it is suspended otherwise
- \Box When ready and $\sigma(t) > 0$ the slack stealer is assigned the highest priority and when $\sigma(t) = 0$ the lowest
- \Box Static computation of $\sigma(t)$ for some t is useful but only when the release jitter in the system is very low
 - Under EDF $\sigma(t = 0) = min_i \{ \sigma_i(0) \}$ where $\sigma_i(0) = D_i \sum_{k=1...i} e_k$ for all jobs released in the hyperperiod starting at t = 0

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Computing the slack under FPS /2

- The slack of periodic jobs of τ_i should be computed based on their effective deadline D_i^e
 - \Box For a job of τ_i this occurs at the beginning of the leveli-1 busy period that precedes D_i so that $D_i^e \leq D_i$
- Hence the initial slack $\sigma_{i,j}(0)$ of every periodic job $J_{i,j}$ in the hyperperiod is determined as

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$$max\left(0, D_{i,j}^e - \sum_{k=1}^{i} \left| \frac{D_{i,j}^e}{T_k} \right| C_k \right)$$

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Computing the slack under FPS /1

- The amount of slack an FPS system has in a time interval may depend on *when* the slack is used
- To minimise the response time of an aperiodic job J_a the decision on when to schedule J_a must obviously consider the execution time of J_a
 - □ No slack stealing algorithm under FPS can minimise the response time of *every* aperiodic job even with prior knowledge of their arrival and execution times
 - □ Better not be greedy in using the available slack

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| Handing aperiodic tasks /4

- *Periodic server* (TPS) general model
 - \Box A (T_{ps}, C_{ps}) periodic task scheduled at the highest priority to only execute aperiodic jobs
 - The TPS has a *budget* of C_{ps} time units and a *replenishment period* of length T_{ps}
 - When the TPS is scheduled and executes aperiodic jobs, it consumes its budget at the rate of 1 unit per unit of time
 - Budget exhausted when $C_{ps} = 0$ and replenished at due time
 - □ The TPS is *backlogged* when the aperiodic job queue is nonempty and it is idle otherwise
 - lacktriangle Eligible for execution only when ready, backlogged and $\mathcal{C}_{ps}>0$

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Handing aperiodic tasks /5

- *Polling server* (PS), a simple kind of TPS
 - □ It is given a fixed budget that it uses to serve aperiodic task requests that is replenished at every period
 - □ The budget is immediately consumed if the PS is scheduled while idle
 - Ready periodic tasks if any execute instead
 - □ It is not bandwidth preserving
 - An aperiodic job that arrives just after the PS has been scheduled while idle must wait until the next replenishment time
 - □ Bandwidth-preserving servers need additional rules for consumption and replenishment of their budget

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Handing aperiodic tasks /7

- *Priority Exchange* (PE), similar in principle to DS
 - If PE server is idle when scheduled, it exchanges its own priority with that of the pending periodic task with priority lower than itself and highest amongst all other pending periodic tasks
 - □ The selected periodic task <u>inherits</u> PE's higher priority until an aperiodic task arrives or PE's ready period ends

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Handing aperiodic tasks /6

- *Deferrable Server* (DS), a bandwidth-preserving TPS
 - DS retains its budget if no aperiodic tasks require execution
 - If an aperiodic task requires execution during the server period, it can be served immediately: the DS does not sleep when idle but stays ready to serve
 - □ The budget is replenished at the start of the new period (!)
 - If an aperiodic request arrives ε time units before the end of T_{ds} the
 request begins to be served and blocks periodic tasks; when the budget
 is replenished new aperiodic requests may be served for the full budget
 - DS worst-case contribution to $\omega(t)$ is $C_{ds} + \left[\frac{t C_{ds}}{T_{ds}}\right] C_{ds}$ delaying hard tasks <u>longer</u> than one server budget per period

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| Handing aperiodic tasks /8

- *Sporadic Server* (SS), fixes the bug in DS
 - □ The budget is replenished <u>only when exhausted</u> and at a minimum guaranteed distance from its earlier execution
 - Hence not periodically!
 - □ This places a tighter bound on its interference and makes schedulability analysis simpler and less pessimistic
- This is the default server policy in POSIX

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SS rules under FPS

■ Consumption rules

 \Box At time $t > t_r$ where t_r is the latest replenishment time a backlogged SS consumes budget only if it is executing or no higher-priority task is ready

■ Replenishment rules

- \Box t_r is recorded at the time that SS' budget is set to C_{ss}
 - $t_r = 0$ when the system begins execution
- \Box The effective replenishment time t_e , the time at which SS should become running, is determined at time t_f when SS first begins to execute since t_r
 - t_e is set to the latest time instant at which a lower-priority task executes in (t_r, t_f) or to t_r if higher-priority tasks had been busy in that interval
 - The next replenishment time is set to $t_e + T_{ss}$

■ Exception

 \Box If $t_e + T_{ss} < t_f$ SS is late and budget is replenished as soon as exhausted

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Handing aperiodic tasks /9

- SS is more complex than PS or DS
 - □ Its rules require keeping tab of a lot of data, several cases to consider when making scheduling decisions
 - This complexity is acceptable because the schedulability of a SS is easy to demonstrate
 - SS under FPS can be seen just like a periodic task τ_s with (p_s, e_s)
- Under EDF or LLF scheduling we can use a dynamic variant of SS as well as other bandwidth-preserving server algorithms
 - □ Constant utilization server
 - □ Total bandwidth server
 - □ Weighted fair queuing server

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Task sets with D < T

- For D = T, Rate Monotonic priority assignment (a.k.a. ordering) is optimal
- For *D* < *T* , *Deadline Monotonic* priority ordering is optimal

$$D_i < D_j \Rightarrow P_i > P_j$$

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DMPO is optimal /1

- Deadline monotonic priority ordering (DMPO) is optimal
 - any task set Q that is schedulable by priority-driven scheme W it is also schedulable by DMPO
- The proof of optimality of DMPO involves transforming the priorities of *Q* as assigned by *W* until the ordering becomes as assigned by DMPO
- Each step of the transformation will preserve schedulability

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DMPO is optimal /2

- Let τ_i , τ_j be two tasks with adjacent priorities in Q such that under W we have $P_i > P_j \land D_i > D_j$
- Define scheme W' to be identical to W except that tasks τ_i , τ_j are swapped
- Now consider the schedulability of Q under W'
- All tasks $\{\tau_k\}$ with priority $P_k > P_j$ will be unaffected
- All tasks $\{\tau_s\}$ with priority $P_s < P_i$ will be unaffected as they will experience the same interference from τ_i and τ_i
- Task τ_j which was schedulable under W, now has a higher priority, suffers less interference, and hence must be schedulable under W'

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DMPO is optimal /3

- All that is left to show is that task τ_i, which has had its priority lowered, is still schedulable
- Under W we have $R_i \leq D_i$, $D_i < D_i$ and $R_i \leq T_i$
- Task τ_j only interferes once during the execution of task τ_i hence $R_i' = R_i \le D_i < D_i$
 - \Box Under W' task au_i completes at the time task au_i did under W
 - ullet Hence task au_i is still schedulable after the switch
- Priority scheme W' can now be transformed to W" by choosing two more tasks that are in the wrong order for DMPO and switching them

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Summary

- A simple (periodic) workload model
- Delving into fixed-priority scheduling
- A (rapid) survey of schedulability tests
- Some extensions to the workload model
- Priority assignment techniques

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