8.a Multicore systems – initial reckoning

Credits to A. Burns and A. Wellings



to B. Andersson and J. Jonsson for their work in *Proc. of the the IEEE Real-Time Systems Symposium*, WiP Session, 2000, pp. 53–56

and to a student of this class a few years back

Hardware architecture taxonomy

- A multiprocessor (or multi-core) is tightly coupled
 - Global status and workload information on all processors (cores) can be kept current at low cost
 - □ The system may use a centralized dispatcher and scheduler
 - □ When each processor (core) has its own scheduler, the decisions and actions of all schedulers are coherent
 - Scheduling in this model is an NP-hard problem
- A distributed system is *loosely coupled*
 - □ It is too costly to keep global status
 - □ There usually is a dispatcher / scheduler per processor

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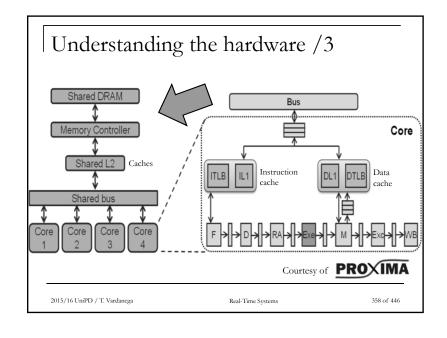
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Fundamental issues

- Hardware architecture taxonomy
 - □ Homogeneous vs. heterogeneous processors
 - Research focused first on SMP (symmetric multiprocessors) that make a much simpler problem
- Scheduling approach
 - Global or partitioned or alternatives between these extremes
 - Partitioning = allocation problem followed by single-CPU scheduling
- Optimality criteria are shattered
 - □ EDF no longer optimal and not always better than FPS
 - Global scheduling not always better than partitioned

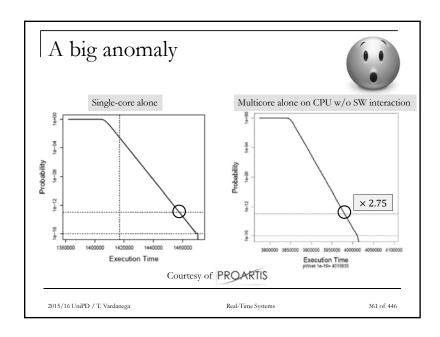
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Hardware interference /1

- Parallel execution on a multiprocessor causes vast opportunities of contention for hardware resources that are shared among the cores
- This phenomenon increases the execution time of running threads by causing them to hold the CPU *without* progressing (!)
 - □ Unlike software interference, which prevents a ready thread from running

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Hardware interference /2 ■ The WCET of a simple single-path program running alone does not stay the same when other programs happen to execute on other CPUs Courtesy of PROARTIS Real-Time Systems 360 of 446

State of the art: what a loss!



- Some task sets may be deemed unschedulable even though they have low utilization
 - Much less than linear with the number of processors
 - □ This is known as the Dhall's effect [Dhall & Liu, 1978]
- The known *exact* schedulability tests have exponential time complexity
 - The known sufficient tests have polynomial time complexity but obviously are pessimistic
- Rate-monotonic priority assignment is not optimal
- No optimal priority assignment scheme with polynomial time complexity has been found yet

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Simplifying assumptions

- Processor (CPU) identity
 - □ All processors are equivalent
- Task independence
 - □ Tasks are logically independent of one another
- Task unity
 - Tasks have no internal parallelism: they can run only on one CPU at any one time
- Task migration
 - □ Tasks can run on different CPUs at different times
- No overhead
 - Context switch and migration costs are built into WCET estimates

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The solution space for scheduling Global Partitioned Task set Task set

Predictability [Ha & Liu, 1994]

- For arbitrary job sets on multiprocessors, if the scheduling algorithm is *work-conserving*¹⁾, preemptive, global (with migration), with fixed job priorities is predictable
 - Job completion times monotonically related to job execution times
- Hence it is safe to consider only upper bounds for job execution times in schedulability tests
- This is <u>not true</u> for non-preemptive scheduling
 - A scheduling algorithm is work conserving if processors are not idle while tasks eligible for execution are not able to execute on other processors

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Software interference /1

- We know what is the interference I_i suffered by a task τ_i for single-processor scheduling
 - □ How does this change for multiprocessors?
- For *global* multiprocessor scheduling with m
 processors interference only occurs for tasks from m + 1 onward
- Multiprocessor interference can be computed as the sum of all intervals when *m* higher-priority tasks execute <u>in parallel</u> on all *m* processors

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Software interference /2

 A very pessimistic bound considers all higherpriority tasks to always fully interfere

$$\square R_k^{max} = C_k + \left(\frac{1}{m} \sum_{\tau_j \in hp(k)} \left(\left\lceil \frac{R_k^{max}}{T_j} \right\rceil C_j + C_j \right) \right)$$

■ This naive bound can be improved, and has been, but for great computational complexity and still without becoming exact

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Dhall's effect /2

Task	T	D	С	U
d	10	10	9	0.9
e	10	10	9	0.9
f	10	10	2	0.2

On 2 processors $\sum U_i = 2$

- Partitioned scheduling does not work here either
- After tasks d and e are allocated, task f cannot reside on just one processor
 - ☐ It needs to migrate from one to the other to find room for execution
- And it also needs that tasks d and e are willing to use cooperative scheduling for it complete in time

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Dhall's effect /1

Task	T	D	С	U
a	10	10	5	0.5
b	10	10	5	0.5
с	12	12	8	0.67

On 2 processors
$$\sum_{i} U_i = 1.67 < 2$$

- Under global scheduling, EDF and FPS would run tasks **a** and **b** first on each of the 2 processors
- But this would leave no time for task **c** to complete

 7 time units on each processor, 14 in total, but 8 on neither
- Even if the total system is underutilized (!)

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Global scheduling anomalies

- In single-processor real-time scheduling the deadline miss ratio often highly depends on the system load
 - □ This suggests that increasing the period should decrease the utilization and thus decrease the deadline miss ratio

Anomaly 1

□ A *decrease* in processor demand from higher-priority tasks can *increase* the interference on lower-priority tasks because of the change in the time when tasks execute

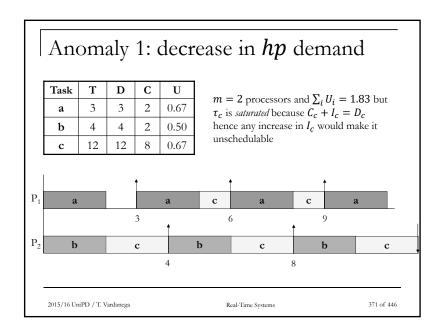
■ Anomaly 2

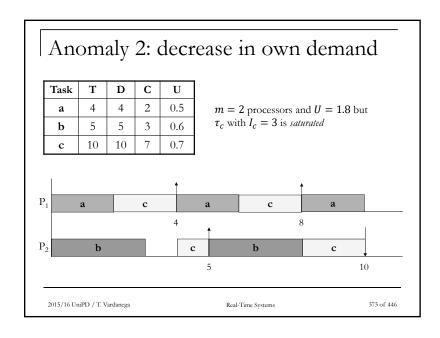
□ A decrease in processor demand of a task causes an *increase* in the interference suffered by that task

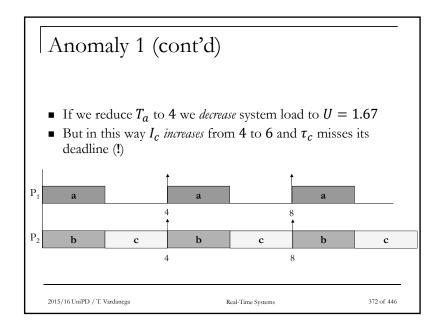
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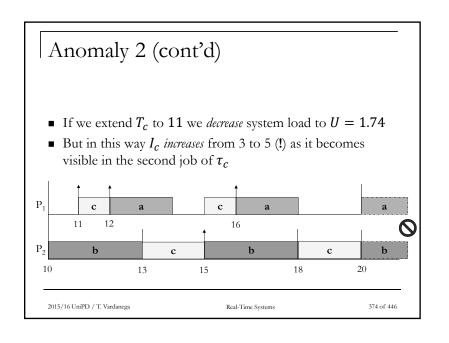
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The defeat of greedy schedulers

- Greedy algorithms are easy to explain, study, and implement
 - □ They work very well on single-core processors
 - □ EDF [1] and LLF [2] are optimal for single-core processors
- They collapse the urgency of a job into a single value and use it to greedily schedule jobs
- Unfortunately (and surprisingly) greedy algorithms fail when used on multiprocessors
 - □ EDF and LLF are no longer optimal

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P-fair scheduling [Baruah et al. 1996]

- Proportional progress is a form of proportionate fairness also known as **P-fairness**
 - \Box Each task τ_i is assigned resources in proportion to its *weight* $W_i = \frac{c_i}{T_i}$ so that it progresses proportionately
 - □ Useful e.g., for real-time multimedia applications
- At every time t task τ_i must have been scheduled either $|W_i \times t|$ or $[W_i \times t]$ time units
 - □ Without loss of generality, preemption is assumed to only occur at integral time units
 - □ The workload model is assumed to be periodic

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Why do greedy schedulers fail?

Theorem 1 (stating the obvious)

When the total utilization of a periodic task set is equal to the number of processors, then no feasible schedule can allow any processor to remain idle for any length of time

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P-fair scheduling /2

- $lag(S, \tau_i, t)$ is the difference between the total resource allocation that task τ_i should have received in [0, t) and what it received under schedule S
- \blacksquare For a P-fair schedule S at time t
 - $\neg \tau_i$ is ahead iff $lag(S, \tau_i, t) < 0$
 - $\Box \tau_i$ is behind iff $lag(S, \tau_i, t) > 0$
 - $\Box \tau_i$ is punctual iff $lag(S, \tau_i, t) = 0$

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P-fair scheduling /3

- $\alpha(x)$ is the *characteristic* (infinite) *string* of task τ_x over $\{-, 0, +\}$ for $t \in \mathbb{N}$ with
 - - Distance from the integral approximation of fluid curve
 - $\alpha(x,t)$ is the *characteristic substring* $\alpha_{t+1}(x)\alpha_{t+2}(x)...\alpha_{t}(x)$ of task τ_x at time t where $t'=min i: i>t: \alpha_i(x)=0$
- For a P-fair schedule S at time t, task τ_i is
 - \Box Urgent iff τ_i is behind and $\alpha_t(\tau_i) \neq -$
 - \Box Tnegru iff τ_i is ahead and $\alpha_t(\tau_i) \neq +$
 - □ *Contending* otherwise

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P-fair scheduling /4

- General principle of P-fairness
 - Every task *urgent* at time t must be scheduled at t to preserve P-fairness
 - □ No task *tnegru* at time *t* can be scheduled at *t* without breaking P-fairness
- Problems with n_0 tnegru, n_1 contending, n_2 urgent tasks at time t, with m resources and $n = n_0 + n_1 + n_2$

 - □ If $n_0 > n m$ the scheduling algorithm is forced to schedule some *tnegru* tasks

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Properties of a P-fair schedule S

■ For task τ_i ahead at time t under S

Integring $\{ u \in \mathcal{T}_t(\tau_i) = -\text{ and } \tau_i \text{ not scheduled at } t \text{ then } \tau_i \text{ is } ahead \text{ at } t+1 \}$ $\{ u \in \mathcal{T}_t(\tau_i) = 0 \text{ and } \tau_i \text{ not scheduled at } t \text{ then } \tau_i \text{ is } punctual \text{ at } t+1 \}$ $\{ u \in \mathcal{T}_t(\tau_i) = +\text{ and } \tau_i \text{ not scheduled at } t \text{ then } \tau_i \text{ is } behind \text{ at } t+1 \}$ $\{ u \in \mathcal{T}_t(\tau_i) = +\text{ and } \tau_i \text{ not scheduled at } t \text{ then } \tau_i \text{ is } ahead \text{ at } t+1 \}$ $\{ u \in \mathcal{T}_t(\tau_i) = +\text{ and } \tau_i \text{ scheduled at } t \text{ then } \tau_i \text{ is } ahead \text{ at } t+1 \}$

- For task τ_i behind at time t under S
 - \Box If $\alpha_t(\tau_i) = -$ and τ_i scheduled at t then τ_i is ahead at t+1
 - \Box If $\alpha_t(\tau_i) = -$ and τ_i not scheduled at t then τ_i is behind at t+1
- $\begin{cases}
 \Box & \text{If } \alpha_t(\tau_i) = 0 \text{ and } \tau_i \text{ scheduled at } t \text{ then } \tau_i \text{ is } punctual \text{ at } t+1 \\
 \Box & \text{If } \alpha_t(\tau_i) = + \text{ and } \tau_i \text{ scheduled at } t \text{ then } \tau_i \text{ is } behind \text{ at } t+1
 \end{cases}$

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P-fair scheduling /5

- The **PF** scheduling algorithm
 - □ Schedule all *urgent* tasks
 - □ Allocate the remaining resources to the highest-priority contending tasks according to the total order function ⊇ with ties broken arbitrarily
 - $x \supseteq y \text{ iff } \alpha(x,t) \ge \alpha(y,t)$
 - And the comparison between the characteristics substrings is resolved lexicographically with −< 0 < +
- With PF we have $\sum_{x \in [0,n]} W_x = m$
 - A dummy task may need to be added to the task set to top utilization up
- No problem situation can occur with the PF algorithm

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Example (PF scheduling) /1

Task	С	T	W
v	1	3	0.333
w	2	4	0.5
x	5	7	0.714
y	8	11	0.727
z	335	462	3-U

- m = 3 processors
- n = 4 tasks
- τ_z is a dummy task used to top system utilization up
- In general its period is set to the system hyperperiod
 - ☐ This time we halved it
- With PF we always have $n_2 > m$ and $n_0 \le n m$

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				П	These task	s are s	chedul	led and	they b	oecome	ahead		
	lag × period				characteristic string				ring	urgent	contending	tnegru	
t	v	w	x	y	2	v	w	x	y	z	tasks	tasks	tasks
0	0	0	0	0	0	-					-{}	y > z > x > w > v	-{}-
1	1	2	-2	-3	-127	-	0	+	+	+	{w}	y>z>x>v	-{}-
2	2	0	3	-6	-254	0	-	+	+	+	$\{v,x\}$	w > y > z	{}
3	0	-2	1	2	81	-	0	-	-	-	-{}	y > z > x > v	$\{w\}$
4	1	0	-1	-1	-46	-	1	+	+	+	{}	y > z > x > v = w	<i>{</i> }
5	2	2	-3	-4	-173	0	0	+	+	+	$\{v, w\}$	y > z > x	{}
6	0	0	13	-7	162	1-	- \	0	+	1+1	$\{x,z\}$	w > y > v	-{}-
7	1	-2	0	1	35	-	0	-			-{}	y>z>x>y	$\{w\}$
8	2	0	-2	75	-92	0	-	+	+	+	$\{v\}$	$y>z>x \not> w$	{}
9	0	2	3	-5	-219	-	0	+	+	+	$\{w, x\}$	y > z > v	{}
10	1	0	1	-8	116	-		+	0		{}	z > x > v = w	{ <i>y</i> }
11	-1	2	-1	0	-\11	0	0	+	-	+	$\{w\}$	y>z>x	$\{v\}$
12	0	0	4	-3	-138	-	-	+	+	+	$\{x\}$	y>z>w>v	-{}-
13	1	2	2	-6	-265	/-	0	0	+	+	$\{w, x\}$	v > y > z	-{}-
14	-1	0	0	2	70	0					{} /	y > z > x > w	$\{v\}$
15	0	2	-2	-1	-57	-	0	+	+	+	{w}	y > z > x > v	{}
16	1	0	3	-4	-184	-	-/	+	+	+	{x}	y > z > v = w	-{}
17	2	2	1	-7	-311	0	0	7	+	+	$\{v, w\}$	x > y > z	-{}-
18	0	0	-1	1	24	-	-	+	+	$ \angle $	{}	y > z > x > w > v	-{}-
19	1	2	-3	-2	-103	-	0	+	A	/+	{w}	y > z > v = x	-{}-