

2. Scheduling issues

Common approaches /2

- **Weighted round-robin scheduling**
 - With basic round-robin (which requires preemption)
 - All ready jobs are placed in a FIFO queue
 - CPU time quantized, that is, allotted in *time slices*
 - The job at head of queue is allowed to execute for one quantum
 - If not complete by end of quantum, it goes to the tail of the queue
 - Hence all jobs in the queue are given one quantum per round
 - Not good for jobs with precedence relations
 - Fine for producer-consumer pipelines that proceed in continual increments
 - With weighted correction (as for the scheduling of network traffic)
 - Jobs are assigned CPU time according a 'weight' (fractionary) attribute
 - Job J_i gets ω_i time slices per round – one round is $\sum_i \omega_i$ of ready jobs

Common approaches /1

- **Clock-driven (time-driven) scheduling**
 - Scheduling decisions are made beforehand (off line) and actuated at fixed time instants
 - The time instants occur at intervals signaled by clock via interrupts
 - The scheduler first dispatches to execution the job due in the current time period and then suspends itself until then next schedule time
 - The scheduled job is supposed to complete before the next schedule time → this scheme requires no preemption
 - All parameters that matter must be known in advance
 - The schedule is computed offline and fixed forever
 - The run-time overhead incurred in its execution is minimal

Common approaches /3

- **Priority-driven (event-driven) scheduling**
 - This class of algorithms is *greedy*
 - Never leave available processing resources unutilized
 - An available resource may stay unused iff there is no job ready to use it
 - A *clairvoyant* alternative may instead defer access to the CPU to incur less contention and thus reduce job response time
 - Anomalies may occur when job parameters change dynamically
 - Scheduling decisions are made at run time when changes occur to the “ready queue”, hence on local knowledge
 - The event causing a scheduling decision is called “*dispatching point*”
 - It includes algorithms also used in non real-time systems
 - FIFO, LIFO, SETF (shortest e.t. first), LETF (longest e.t. first)

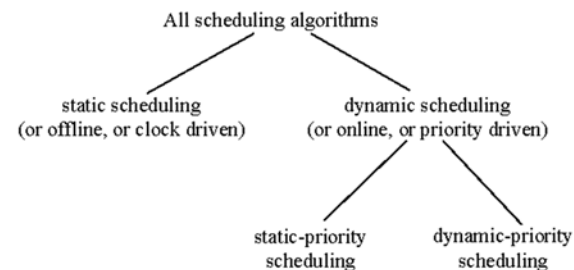
Predictability of execution

- Initial intuition
 - The execution of job set J under a given scheduling algorithm is **predictable** if the actual start time and the actual response time of every job in J vary within the bounds of the *maximal* and *minimal schedule*
 - *Maximal schedule*: the schedule created by the scheduling algorithm under worst-case conditions
 - *Minimal schedule*: analogously for best-case
- **Theorem**: the execution of independent jobs with given release times under preemptive priority-driven scheduling on a single processor *is* predictable

Preemption vs. non preemption /1

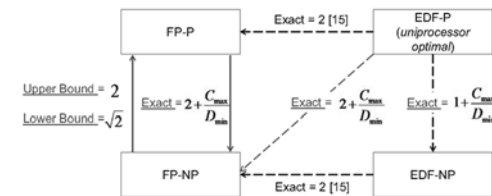
- Can we compare preemptive scheduling with non-preemptive scheduling for performance?
 - There is no single response that is valid in general
 - When all jobs have same release time and preemption overhead is negligible (!?) then preemptive scheduling is provably better
 - It would be interesting to know whether the improvement of the last finishing time (aka *minimum makespan*) under preemptive scheduling pays off the time overhead of preemption
- For 2 CPUs we do know that the minimum makespan for non-preemptive scheduling is never worse than $\frac{4}{3}$ of that for preemptive

Classification of Scheduling Algorithms



Preemption vs. non preemption /2

- The *processor speed-up factor* determines the increase in processor speed that a scheduling algorithm would require to equalize an optimal algorithm of the same class for any task set



Ipavis et al., "Quantifying the Exact Sub-Optimality of Non-Preemptive Scheduling", RTSS 2015

Optimality /1

- Priorities assigned dynamically after *absolute* deadlines
 - Ready queue reordering on job release and job completion
- **Earliest Deadline First** scheduling is *optimal* for single CPU systems with independent jobs and preemption
 - For any job set, EDF produces a feasible schedule if one exists
 - The optimality of EDF breaks under other hypotheses (e.g., no preemption, multicore processing)

Ready queue: $J_1, J_1, J_2, J_3, J_1, J_2$

Absolute deadline $d_i = r_i + D_i$

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Optimality /3

- If the goal is that jobs just make their deadlines, then there is little point in having jobs complete any earlier
 - The **Latest Release Time** algorithm (converse of EDF) follows this logic and schedules jobs backwards from the latest deadline
 - LRT operates backward treating deadlines as release times and release times as deadlines
 - LRT is *not* greedy: it may leave the CPU unused with ready tasks
- Greedy scheduling algorithms may cause jobs to suffer larger interference

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Optimality /2

- Priorities assigned dynamically after *laxity* $L(t)$
 - $L_i(t) = (r_i + D_i) - t - R_i(t)$, where $R_i(t)$ is the residual execution time needed for τ_i at time t
 - Scheduling occurs on job release and job completion
 - Jobs' priority, $L(t)$, varies with t : more dynamic than EDF and more costly to implement
- **Least Laxity First** scheduling is optimal under the same hypotheses as for EDF optimality

Ready queue: J_1, J_2, J_1

$L_1(t) = (r_1 + D_1) - t - (e_1 - e_{1_1})$

$L_2(t) = (r_2 - D_2) - t - (e_2 - 0)$

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Latest Release Time scheduling

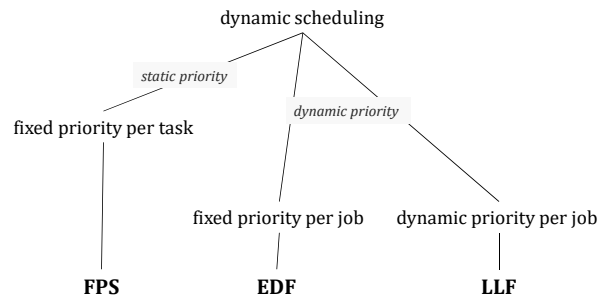
| | T1 | T2 | T3 |
|---|----|----|----|
| A | 0 | 11 | 12 |
| C | 4 | 3 | 4 |
| D | 20 | 18 | 17 |

(D=absolute deadline)

Needs preemption and off line decisions

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Ramifications for dynamic scheduling



Clock-driven scheduling / 2

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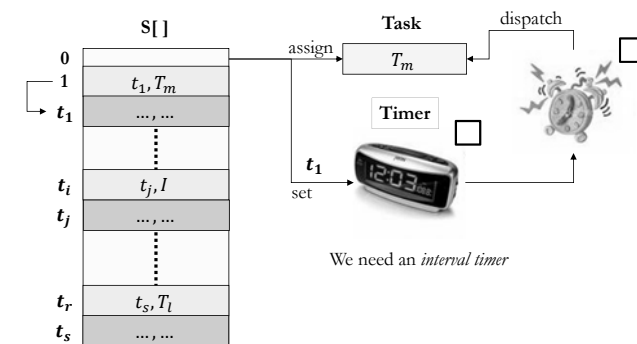
Input: stored schedule  $S(t_k)$  for  $k = \{0, \dots, N - 1\}$ ;  $H$  (hyperperiod)
SCHEDULER:
 $i = 0$ ;  $k = 0$ ; set timer to expire at  $t_k$ ;
do forever:
  sleep until timer interrupt;
  if an aperiodic job is executing
    preempt;
  end if;
  current task  $T = S(t_k)$ ;
   $i = i + 1$ ;  $k = i \bmod N$ ;
  set timer to expire at  $\lfloor i/N \rfloor \times H + t_k$ ; -- at time  $t_k$  in all  $H$  forever
  if current task  $T = I$ 
    execute job at head of aperiodic queue;
  else execute job of task  $T$ ;
  end if;
end do;
end SCHEDULER
  
```

Clock-driven scheduling / 1

Workload model

- N periodic tasks, for N constant and statically defined
 - In Jim Anderson's definition of periodic (not Jane Liu's)
- The $(\varphi_i, p_i, e_i, D_i)$ parameters of every task τ_i are constant and statically known
- The schedule is static and committed off line before system start to a table \mathbf{S} of decision times t_k
 - $S[t_k] = \tau_i$ if a job of task τ_i must be dispatched at time t_k
 - $S[t_k] = I$ (idle) if no job is due
 - Schedule computation can be as sophisticated as we like since we pay for it only once and before execution
 - Jobs *cannot overrun* otherwise the system is in error

Clock-driven scheduling / 3



Example

$(\varphi_i, p_i, e_i, D_i)$

$J = \{t_1 = (0, 4, 1, 4), t_2 = (0, 5, 1.8, 5), t_3 = (0, 20, 1, 20), t_4 = (0, 20, 2, 20)\}$

$U = \sum_i \frac{e_i}{p_i} = 0.76$

$H = 20$

| Time | Schedule |
|------|----------------|
| 0 | t ₁ |
| 1 | t ₃ |
| 2 | t ₂ |
| 3.8 | t ₁ |
| 4 | t ₁ |
| ... | ... |
| 19.8 | t ₁ |
| 20 | Goto t mod(H) |

- The schedule table S for J would need 17 entries
 - That's too many and the schedule too fragmented!
- Why 17?

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Clock-driven scheduling /5

- Constraint 1:** Every job J must complete within f
 - $f \geq \max_{i \in \{1..m\}}(e_i)$ so that *overruns* can be detected
- Constraint 2:** f must be an integer divisor of the hyperperiod
 - $H : H = Nf$ where $N \in \mathbb{N}$
 - It suffices that f be an integer divisor of at least one task period p_i
 - The hyperperiod beginning at minor cycle kf for $k = 0, N - 1, 2N - 1$ is termed *major cycle*
- Constraint 3:** There must be one *full* frame f between J's release time t' and its deadline: $t' + D_j \geq t + 2f$
 - So that J can be scheduled in that frame
 - This can be expressed as: $2f - \text{gcd}(p_i, f) \leq D_i$ for every task τ_i

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Clock-driven scheduling /4

- Reasons of complexity control suggest minimizing the size of the cyclic schedule (table S)
 - The scheduling point t_k should occur at regular intervals
 - Each such interval is termed *minor cycle (frame)* and has duration f
 - We need a (cheaper, more standard) *periodic timer* instead of a (more costly) interval timer
 - Within minor cycles there is no preemption, but a single frame may allow the execution of multiple (run-to-completion) jobs
 - For every task τ_i , φ_i must be a non-negative integer multiple of f
 - Forcedly, the first job of every task has its release time set at the start edge of a minor cycle
- To build such a schedule, we must enforce some constraints

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Understanding constraint 3

Constraint 3

This is the frame in which job J must be scheduled

$t + 2f \leq t' + D_j$

$t' - t \geq \text{gcd}(p_j, f)$

$2f - \text{gcd}(p_j, f) \leq D_j$

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Example

- $T = \{(0, 4, 1, 4), (0, 5, 2, 5), (0, 20, 2, 20)\}$
- $H = 20$
- [c1] : $f \geq \max(e_i) : f \geq 2$
- [c2] : $\lfloor p_i/f \rfloor - p_i/f = 0 : f = \{2, 4, 5, 10, 20\}$
- [c3] : $2f - \gcd(p_i, f) \leq D_i : f \leq 2$
 - $f = 2 : 4 - \gcd(4,2) \leq 4$ **OK** $f = 5 : 10 - \gcd(4,2) \leq 4$ **KO**
 - $4 - \gcd(5,2) \leq 5$ **OK** $f = 10 : 20 - \gcd(4,2) \leq 4$ **KO**
 - $4 - \gcd(20,2) \leq 20$ **OK**
 - $f = 4 : 8 - \gcd(4,4) \leq 4$ **OK** $f = 20 : 40 - \gcd(4,2) \leq 4$ **KO**
 - $8 - \gcd(5,4) \leq 5$ **KO**

Clock-driven scheduling /6

- To construct a cyclic schedule we must therefore make three design decisions
 - Fix an f
 - Slice (the large) jobs
 - Assign (jobs and) slices to minor cycles
- There is a very unfortunate inter-play among these decisions
 - Cyclic scheduling thus is very fragile to any change in system parameters

Clock-driven scheduling /5

- It is very likely that the original parameters of some task set T may prove unable to satisfy all three constraints for any given f simultaneously
- In that case we must decompose task τ_i 's jobs by **slicing** their (WCET) e_i^W into fragments small enough to artificially yield a "good" f

Clock-driven scheduling /7

```

Input: stored schedule S(k) for k = 0,..,F-1;
CYCLIC_EXECUTIVE:
t := 0; k := 0;
do forever:
  sleep until clock interrupt @ time t × f;
  currentBlock = S(k);
  t := t+1; k := t mod F;
  if last job not completed take action;
  end if;
  execute slices in currentBlock;
  while the aperiodic job queue is not empty do
    execute aperiodic job at top of queue;
  end do;
end do;
end SCHEDULER

```

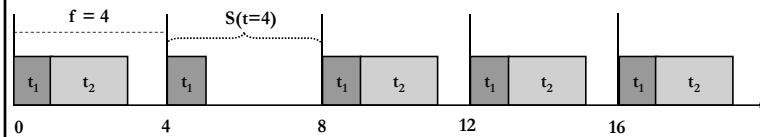
Example (slicing) – 1/2

$$(\varphi_i, p_i, e_i, D_i)$$

$$J = \{\tau_1 = (0, 4, 1, 4), \tau_2 = (0, 5, 2, 7), \tau_3 = (0, 20, 5, 20)\}, H = 20$$

τ_3 causes disruption since we need $e_3 \leq f \leq 4$ to satisfy c3

We must therefore slice e_3 : how many slices do we need?



We first look at the schedule with $f = 4$ and $F = \left(\frac{H}{f}\right) = 5$

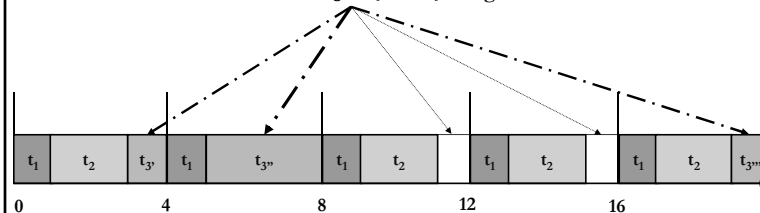
without τ_3 , to see what least-disruptive opportunities we have ...

Design issues /1

- Completing a job much ahead of its deadline is of no use
- If we have spare time we might give aperiodic jobs more opportunity to execute hence make the system more responsive
- The principle of **slack stealing** allows aperiodic jobs to execute in preference to periodic jobs when possible
 - Every minor cycle include some amount of slack time not used for scheduling periodic jobs
 - The slack is a *static* attribute of each minor cycle
- A scheduler does slack stealing if it assigns the available slack time at the beginning of every minor cycle (instead of at the end)
 - However, this value-added provision requires a fine-grained interval timer (again!) to signal the end of the slack time for each minor cycle

Example (slicing) – 2/2

... then we observe that $e_3 = \{1, 3, 1\}$ is a good choice



$$\tau_3 = \{\tau_3' = (0, 20, 1, x), \tau_3'' = (0, 20, 3, y), \tau_3''' = (0, 20, 1, 20)\}$$

where $x < y \leq 20$ represent the precedence constraints that must hold between the slices (could have used phases instead)

Design issues /2

- What can we do to handle **overruns**?
 - Halt the job found running at the start of the new minor cycle
 - But that job may not be the one that overrun!
 - Even if it was, stopping it would only serve a useful purpose if producing a late result had no residual *utility*
 - Defer halting until the job has completed all its “critical actions”
 - To avoid the risk that a premature halt may leave the system in an inconsistent state
 - Allow the job some extra time by delaying the start of the next minor cycle
 - Plausible if producing a late result still had *utility*

Design issues /3

- What can we do to handle *mode changes*?
 - A mode change is when the system incurs some reconfiguration of its function and workload parameters
- Two main axes of design decisions
 - With or without deadline during the transition
 - With or without overlap between outgoing and incoming operation modes

Priority-driven scheduling

- Base principle
 - Every job is assigned a priority
 - The job with the highest priority is selected for execution
- **Dynamic-priority scheduling**
 - Distinct jobs of the same task may have distinct priorities
- **Static-priority scheduling**
 - All jobs of the same task have one and same priority

Overall evaluation

- **Pro**
 - Comparatively simple design
 - Simple and robust implementation
 - Complete and cost-effective verification
- **Con**
 - Very fragile design
 - Construction of the schedule table is a NP-hard problem
 - High extent of undesirable architectural coupling
 - All parameters must be fixed a priori at the start of design
 - Choices may be made arbitrarily to satisfy the constraints on f
 - Totally inapt for sporadic jobs

Dynamic-priority scheduling

- Two main algorithms are champions of that category
 - **Earliest Deadline First** (EDF)
 - **Least Laxity First** (LLF)
- **Theorem** [Liu, Layland: 1973] EDF is optimal for independent jobs with preemption
 - Also true for task sets that sporadic jobs
 - The relative deadline for periodic tasks may be arbitrary with the respect to period ($<$, $=$, $>$)
- Result trivially applicable to LLF
- EDF is *not* optimal for jobs that do *not* allow preemption
 - Preemption is an aid to optimality



Static (fixed)-priority scheduling (FPS)

- Two main variants with respect to the strategy for priority assignment
 - **Rate monotonic**
 - A task with lower period (faster rate) gets higher priority
 - **Deadline monotonic**
 - A task with higher urgency (shorter deadline) gets higher priority
 - What about “*execution-monotonic*”?
- Before looking at those strategies in more detail we need to fix some basic notions

Dynamic scheduling: comparison criteria /2

- **Theorem** [Liu, Layland: 1973] for single processors the schedulable utilization of EDF is 1
- For arbitrary deadlines, the **density**

$$\delta_k = \frac{e_k}{\min(p_k, D_k)}$$
 becomes an important factor to feasibility
 - As $\Delta = \sum_k \delta_k > U$ when $D_i < p_i$ for some τ_i , then $\Delta \leq 1$ becomes a sufficient *schedulability test* for EDF

Dynamic scheduling: comparison criteria /1

- Priority-driven scheduling algorithms that disregard job urgency (deadline) perform poorly
 - The WCET is not a factor of interest for priority!
- How to compare the performance of scheduling algorithms?
- **Schedulable utilization** is a useful criterion
 - A scheduling algorithm can produce a feasible schedule for a task set T on a single processor if $U(T)$ does not exceed its schedulable utilization

Dynamic scheduling: comparison criteria /3

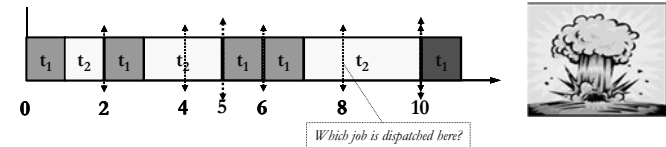
- The schedulable utilization criterion alone is not sufficient: we must also consider predictability
 - Recall its intuition at page 118
- On transient overload the behavior of static-priority scheduling can be determined a-priori and is reasonable
 - The overrun of any job of a given task τ does not harm the tasks with higher priority than τ
- Under transient overload EDF becomes unstable
 - A job that missed its deadline is *more urgent* than a job with a deadline in the future: one lateness may cause many more!

Dynamic scheduling: comparison criteria /4

- Other figures of merit for comparison exist
 - **Normalized Mean Response Time** (NMRT)
 - Ratio between the job response time and the CPU time actually consumed for its execution
 - The larger the NMRT value, the larger the task idle time
 - **Guaranteed Ratio** (GR)
 - Number of tasks (jobs) whose execution can be guaranteed versus the total number of tasks that request execution
 - **Bounded Tardiness** (BT)
 - Number of tasks (jobs) whose tardiness can be guaranteed to stay within given bounds
 - With BT, soft real-time systems can have some utility

Example (EDF) /2

$(\varphi_i, p_i, e_i, D_i)$
 $T = \{t_1 = (0, 2, 1, 2), t_2 = (0, 5, 3, 5)\} \Rightarrow U(t) = \frac{e_1}{p_1} + \frac{e_2}{p_2} = 1.1$
 T has no feasible schedule: what job suffers most under EDF?

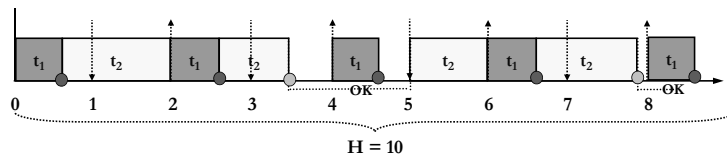


$T = \{t_1 = (0, 2, 0.8, 2), t_2 = (0, 5, 3.5, 5)\} \Rightarrow U(t) = \frac{e_1}{p_1} + \frac{e_2}{p_2} = 1.1$
 T has no feasible schedule: what job suffers most under EDF?

What about
 $T = \{t_1 = (0, 2, 0.8, 2), t_2 = (0, 5, 4, 5)\}$ with $U(t) = \frac{e_1}{p_1} + \frac{e_2}{p_2} = 1.2$?

Example (EDF) /1

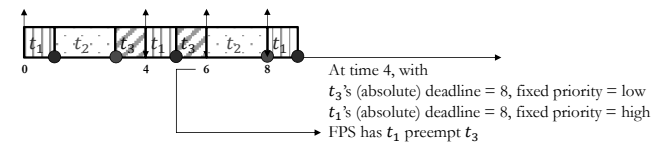
$(\varphi_i, p_i, e_i, D_i)$
 $T = \{\tau_1 = (0, 2, 0.6, 1), \tau_2 = (0, 5, 2.3, 5)\}$
 Density $\Delta(T) = \frac{e_1}{D_1} + \frac{e_2}{D_2} = 1.06 > 1$
 Utilization $U(T) = \frac{e_1}{p_1} + \frac{e_2}{p_2} = 0.76 < 1$
 What happens to T under EDF?



Example (EDF vs FPS) /3

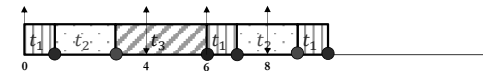
$T = \{t_1 = (0, 4, 1, 4), t_2 = (0, 6, 2, 6), t_3 = (0, 8, 3, 8)\}, U = \frac{23}{24}, H = 24$

With fixed-priority scheduling (FPS), rate-monotonic priority assignment



At time 4, with t_3 's (absolute) deadline = 8, fixed priority = low t_1 's (absolute) deadline = 8, fixed priority = high FPS has t_1 preempt t_3

With earliest-deadline first (EDF)



t_2 's (absolute) deadline = 12, fixed priority = medium FPS has t_2 preempt t_3 , which misses its deadline

Critical instant /1

- Feasibility and schedulability tests must consider the **worst case** for all tasks
 - The worst case for task τ_i occurs when the worst possible relation holds between its release time and that of all higher-priority tasks
 - The actual case may differ depending on the admissible relation between D_i and p_i
- The notion of **critical instant** – if one exists – captures the worst case
 - The response time R_i for a job of task τ_i with release time on the critical instant is the longest possible value for τ_i

Time-demand analysis /1

- When φ is 0 for all jobs considered, this equation captures the *absolute worst case* for task τ_i
- This equation stands at the basis of **Time Demand Analysis**, which investigates how ω varies as a function of time
 - As long as $\omega(t) \leq t$ for *some (important) t* for the job of interest, the supply satisfies the demand, hence the job can complete in time
- **Theorem** [Lehoczky, Sha, Ding: 1989] condition $\omega(t) \leq t$ is an *exact feasibility test* (necessary and sufficient)
 - The obvious question is for which ‘t’ to check
 - The method proposes to check at *all periods of all higher-priority tasks* until the deadline of the task under study

Critical instant /2

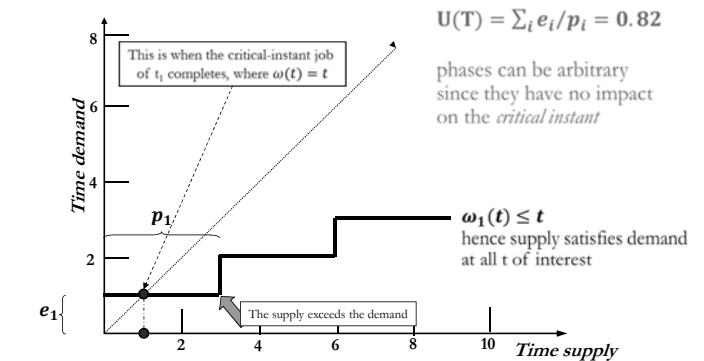
- **Theorem**: under FPS with $D_i \leq p_i \forall i$, the critical instant for task τ_i occurs when the release time of *any* of its jobs is in phase with a job of every higher-priority task in the set
- We seek $\max(\omega_{i,j})$ for all jobs $\{j\}$ of task τ_i for

$$\omega_{i,j} = e_i + \sum_{(k=1, \dots, i-1)} \left\lceil \frac{(\omega_{i,j} + \varphi_i - \varphi_k)}{p_k} \right\rceil e_k - \varphi_i$$

For task indices assigned in decreasing order of priority
- The \sum component captures the **interference** that any job j of task τ_i incurs from jobs of higher-priority tasks $\{\tau_k\}$ between the release time of the first job of task τ_k (with phase φ_k) to the response time of job j , which occurs at $\varphi_i + \omega_{i,j}$

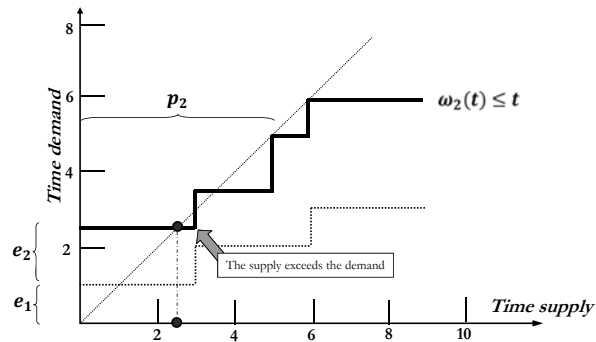
Time demand analysis /2

$T = \{\tau_1 = (-, 3, 1, 3), \tau_2 = (-, 5, 1.5, 5), \tau_3 = (-, 7, 1.25, 7)\}$ $(\varphi_i, p_i, e_i, D_i)$



Time demand analysis /3

$$T = \{t_1 = (-, 3, 1, 3), t_2 = (-, 5, 1.5, 5), t_3 = (-, 7, 1.25, 7)\}$$



Time demand analysis /5

- It is straightforward to extend TDA to determine the *response time* of tasks

The smallest value t that satisfies

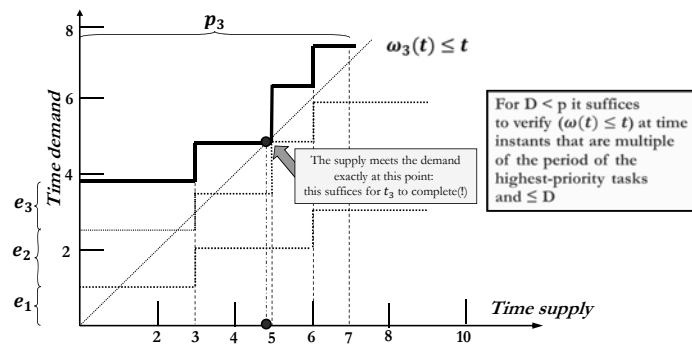
$$t = e_i + \sum_{(k=1, \dots, i-1)} \left\lfloor \frac{t}{p_k} \right\rfloor e_k$$

is the *worst-case response time* of task τ_i

- Solutions methods to calculate this value were independently proposed by
 - [Joseph, Pandia: 1986]
 - [Audley, Burns, Richardson, Tindell, Wellings: 1993]

Time demand analysis /4

$$T = \{t_1 = (-, 3, 1, 3), t_2 = (-, 5, 1.5, 5), t_3 = (-, 7, 1.25, 7)\}$$



Time demand analysis /6

- What changes in the definition of critical instant when $D > p$?
- Theorem** [Lehoczky, Sha, Strosnider, Tokuda: 1991] The first job of task τ_i may *not* be the one that incurs the worst-case response time
- Hence we must consider *all* jobs of task τ_i within the so-called *level- i busy period*
 - The (t_0, t) time interval within which the processor is busy executing jobs with priority $\geq i$, release time in (t_0, t) , response time falling within t
 - The release time in (t_0, t) captures the full backlog of interfering jobs
 - The response time of all those jobs falling within t ensures that the busy period includes their completion

Example

$T_1 = \{-, 70, 26, 70\}, T_2 = \{-, 100, 62, 120\}$ (φ_i, p_i, e_i, D_i)
 Let's look at the level-2 busy period

Ready queue: $J_{1,1}, J_{2,1}$
 Time window 1 [0,70]
 Time left for $J_{2,1}$: $70-26 = 44$
 Still to execute: $62-44 = 18$

Ready queue: $J_{1,2}, J_{2,1}$
 Time window 2 [70,100]
 Time left for $J_{2,1}$: $30-26 = 4$
 Still to execute: $18-4 = 14$
 Release time of job $J_{2,2}$

Ready queue: $J_{2,1}, J_{2,2}$
 Time window 3 [100,140]
 Time left for $J_{2,1}$: 40
 $J_{2,1}$ completes at: 114 ($R = 114$)
 Time available for $J_{2,2}$: $40-14 = 26$
 Still to execute: $62-26 = 36$

Ready queue: $J_{2,2}, J_{2,3}$
 Time window 5 [200,210]
 Release time of job $J_{2,3}$
 $J_{2,2}$ completes at: 202 ($R = 102$)
 Time available for $J_{2,3}$: $10-2 = 8$
 Still to execute: $62-8 = 54$

Ready queue: $J_{1,2}, J_{2,2}$
 Time window 4 [140,200]
 Time available for $J_{2,2}$: $60-26 = 34$
 Still to execute: $36-34 = 2$

Ready queue: $J_{1,2}, J_{2,3}$
 Time window 6 [210,280]
 Time available for $J_{2,3}$: $70-26 = 44$
 Still to execute: $54-44 = 10$

Ready queue: $J_{1,3}, J_{2,3}$
 Time window 7 [280,300]
 Time available for $J_{2,3}$: $20-20 = 0$
 Release time of job $J_{2,4}$

Still in ready queue: $J_{2,4}$
 Time window 8 [300,350]
 Time available for $J_{2,3}$: $50-6 = 44$
 $J_{2,3}$ completes at: $300+6+10 = 316$ ($R = 116$)
 $J_{2,1}$'s response time is **not** worst-case!

The T_2 busy period extends beyond this point (!)

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Summary

- Initial survey of scheduling approaches
- Important definitions and criteria
- Detail discussion and evaluation of main scheduling algorithms
- Initial considerations on analysis techniques

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Level-i busy period

$T_1 = \{-, 100, 20, 100\}, T_2 = \{-, 150, 40, 150\}, T_3 = \{-, 350, 100, 350\} \Rightarrow U = 0.75$
 The same definition of level-i busy period holds also for $D \leq p$
 but its width is obviously shorter!

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Selected readings

- T. Baker, A. Shaw
The cyclic executive model and Ada
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- C.L. Liu, J.W. Layland
Scheduling algorithms for multiprogramming in a hard-real-time environment
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